

ARTS4201

I gYgʻcZH\Ycfm`<cbci fgʻfF YgYUfVXŁ

7 ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`q

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
GYUb Dfmcf	g"dfmcf4 i bgk "YXi "Ui	-	FcVYfh KYVghYf`&%	-',) +'%)

GW.cc`7cbhJWh =bZcfa Uhlcb

Fcca " %&ž"Yj Y" FcVYfhK YVqhYf'6i]X]b[

D\cbY. f\$&Ł'-',) '(,)*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVq]hY. \hada.#qUa "Ufhq"i bgk "YXi "Ui_

H\Y'GW\cc``cZh\Y'5fhg'UbX'A YX]U'k ci `X'`]_Y'hc'F YgdYWMZ ``m'5W_bck `YX[Y'h\Y'HfUX]h]cbU``7i qhcX]Ubqž h\Y'6YXY[U`fPYbq]b[hcb'WJa di qŁž; UX][U`f7]hmUbX'5fh/ '8Yq][b'7Ua di qYqŁ'UbX'h\Y'B[i bbUk U` dYcdYffuEcZh\Y "UbXgk\YfYYUW\ WJa digcZl BGK]g `cWJhYX"

5 h Y b X U b W F Y e i] f Y a Y b h g

5 qh XYbh]q Yl dYWYX hc UhYbX U``WUqq WcbhUWi\ci fq Zcf U ZUW!hc! ZUW! fl & L'cf V YbXYX Wci fqY UbX Wca d`YhY'U```UWhjj]hjYg'Zcf'U'V`YbXYX'cf'Zl ``micb`]bY'Wci fgY"

5 'ghi XYbhik \c'Uff]j Yg'a cfY'h\Ub'%) 'a]bi hYg'`UhY'a UmVY'dYbU`]gYX'Zcf'bcb!UhhYbXUbWY'''⊋qi W\'U'dYbU`hm]g^]a dcgYXžh\Y^gh XYbha i ghVY^]bZcfa YX^j YfVU``mUhh\Y^YbX`cZWUgg^UbX`UXj]gYX^]b^k f]h|b[^k]h\]b^&(\ci fg"

ZUʻqh XYbhYl dYf[YbWYq']`bYqqža]qUXj Ybh fYʻcfʻch\YfʻcVW ffYbW h\Uha U_YqʻUVqYbW Zfca ʻU Wugg#JWnjj]mmi buj c]XUV`Yžcf`Yl dYWng hc VY`UVgYbhZfca `U`Zcfh\Wca]b[`Wugg#JWnjj]mmzh\Ymg\ci `X`gYY_ dYfa]gg]cb Zfca 'h\Y'7 ci fgY'5i h\cf]mž'UbX'k \YfY'Udd`]WUV`Yž'h\Y]f'fYei Yghg\ci `X'VY'UWWca dUb]YX'VmUb cf][]bU`cf`WfflZYX`WcdmcZU'a YX]WU`WYfhlZWJhY`cf`ch\Yf`Zcfa 'cZUddfcdf]UhY`Yj]XYbWY"

5 7 ci fqY 5 i h\cf|lma UmYl W qY U qhi XYbh2fca WUqqYq cf UWlij |h|Yq Zcf i d hc cbY a cbh\" < ck Y j Yfz h\Ym a Um'Ugg][b'UXX]hcbU`UbX#cf'U`hYfbUh]j Y'hUg_g'hc'Ybgi fY'Wca d`]UbWY"'5'7 ci fgY'5i h\cf]miWcbg]XYf]b['h\Y [fubh]b[cZuvgYbWraighvYguh]gZjYX'u'gh XYbhk]```gh]```vY'uv`Y'hc'a YYhh\Y'WcifgY'g``Yufb]b[cihWcaYg UbX#cf'j c'i a Y'cZ'YUfb]b["'5 'gh XYbhgYY_]b['Uddfcj U'hc'VY'UVgYbhZcf'a cfY'h\Ub'cbY'a cbh\'a i qhUdd`m]b'k f]h]b['hc'h\Y'8YUb'UbX'dfcj]XY'U```cf][]bU``cf'Wfh]ZYX'gi ddcfh]b['XcW a YbhUh]cb"

: cf'a cfY']bZcfa Uhlcb'UVci hih\Y'UhhYbXUbWY'dfchcWc`q']b'h\Y': UW\`hmcZ5fhq'UbX'GcWjU` GWYbWrg. \httq.#k k k "Uffig"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa]W]bZcfa Uhjcb#dfchcWc`g![i]XY`]bYg#

5 WUXYa]W = b Zcfa Uhich

: cf`YggYbhJU``ghi XYbh`]bZcfa UhJcb`fY`UhJb[`hc.`fYei Yghg`Zcf`Yl hYbg]cb/fYj]Yk `cZa Uf_g/cWW dUhJcbU``\YU`h\UbX`gUZ/hm/Yl Ua]bUhJcb'dfcWXi fYg/gdYVJU``Wcbg]XYfUhJcb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybhi fY/ghi XYbhYei]hmUbX`X]gUV]`]hm/UbX`ch\Yf`YggYbhJU``UWUXYa]W]bZcfa UhJcbž gYY`\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhghi XYbhg#JWUXYa]W]bZcfa UhJcb#dfchcWc`g![i]XY`]bYg#

7ci fgY 8YHJ] g

7 fYX]hDc]bhg '%'

Gi a a UfmcZh\Y'7ci fgY

 $H\setminus]g'<cbci\ fg!\ Yj\ Y`gYa\]bUf'Wci\ fgY']g'XYg][\ bYX'hc'Yb[\ U[\ Y'UXj\ UbW'X'ghi\ XYbhg']b'h\ Y'X]gW]d`]bYg'cZ \\ 9b[\]g\setminus Z':\]'a\ Z'A\ YX]UZ'A\ i\ g]W'H\setminus YUHY'UbX'DYfZcfa\ UbW'UbX'8 UbW']b'Ugi\ fj\ YmcZWcbhYa\ dcfUfmW'hi\ fU'h\ Ycfm'UbX']b!XYdh\ 'X]gW]d`]bY!VUgYX'UbU'mg]g'''+\ Y'Wci\ fgY'VY[\]bg'k\]h\ 'Ub']bH'fX]gW]d`]bUfmZcW g'cb W'hi\ fU''h\ Ycfm]b'cfXYf'hc'ZcghYf'U'Z]Y'X'cZWcbW'dhi\ U`'Wca\ a\ cbU']h]Yg'UWfcgg'X]gW]d`]bUfmVci\ bXUf]Yg'''+h\ Yb'gYYg'ghi\ XYbhg'VfYU_']bhc'X]gW]d`]bUfmgi\ V![\ fci\ dg'hc'U``ck'h\ Y'XYVUhYg'k\]h\]b'W'hi\ fU''h\ Ycfmhc]``i\ a\]bUhY'dUfh]W'\UbX'UbU'mh]WU''W\ U``Yb[\ Yg']bhYfbU''hc'YUW\ X]gW]d`]bY''$

5 hh Y WcbWi g]cb cZh]g Wci fgY h Y gh XYbhk]``VY UV Y hc

%" Wcblf]Vi lY ']blY``][Ybhmlc Wf]h]WU`X]gW gg]cbg cZh\Ya Yg 'UbX']ggi Yg 'Wcj YfYX']b 'WUgg &" fYgYUfW. 'UbX'XY`]j Yf'U'Zcfa U``WUgg dfYgYbhUh]cb cb 'Wci fgY 'a UhYf]U` ' " fYgYUfW. 'UbX'k f]hY 'Ub'YI lYbXYX'Wf]h]WU`'UbU`mg]g cZWci fgY 'a UhYf]U` (" a U_Y'a YUb]b[Z ``UbX'_bck `YX[YUV`Y'WcbbYWflcbg VYhk YYb'h\Ycf]Yg 'UbX#cf'hYl hg gh X]YX

HYUWX]b['GhfUhY[]Ya'

H\Y`WcifgY`k]```VY`HJi[\hZ]fghmh\fci[\`'U``Uf[Y`gYa]bUf`Zcf`h\Y`YbhJfY`gW\cc``Wc\cfh`YX`Vm'U`g]b[`Y WcbjYbcfz`Zc``ck YX`Vmga U``Yfz`a cfY`ZcW gYX`X]gWJd`]bUfm[fci dgz``YX`Vm']bX]j]Xi U``Wcbj Ybcfg`Zfca `h\Y X]ZYfYbhX]gWJd`]bYg`UWfcgg`G5A "'H\Y`Wca V]bUhJcb`k]```dfcj]XY`Zcf`h\Y`XYjY`cda YbhcZ]bhYfX]gWJd`]bUfm X]U`c[i Y`UWfcgg`Wc[bUhY`X]gWJd`]bYg`UbX`bYhk cf_g`rc[Yh\Yf`k]h\`hJ[\hX]gWJd`]bY!VUgYX`Wc\cfhg`hc`ZJWJ\]hUhY h\Y`Zck`cZ[YbYfU``h\YcfYhJWJ`Zcfa i `UhJcbg`]bhc`gdYWJU`]ghX]gWJd`]bUfmdfcV`Ya UhJ\wf"

5ggYgga Ybh

 $\label{eq:final_continuous_cont$

Hcd]Wg^k]``VY^X]ghf]Vi hYX^]b^WUgg"

 $\label{thm:condition} \mbox{Hi fb]h]b"gYh]b" Low Ybh"]g"gi Va]hhYX"h\fci [\h]b" Low X"ghi XYbhg"Xc"bchgYY"Hi fb]h]b g]a]"Uf]hm"fYdcfhg" \mbox{Hi fb]h]b" Low Ybh"]g"gi Va]hhYX"h\fci [\h]b" Low Ybh"]g"g [$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gh XYbhg UfY Yl dYWYX hc di hh\Y]f bUa Yg UbX gh XYbhbi a VYfg cb Yj YfmdU[Y cZh\Y]f Ugg][ba Ybhg"

Hi fb]h]b Gi Va]gg]cb

Imagi YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dr]b['rc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]r]bž'd'YUgY hY'Yd\cbY'9I hYfbU'Gi ddcfhcb'-',) "''' %cf'Ya U] hYa 'cb'<u>Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui"</u> "Gi ddcfh \ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'" Imai UfY'i bUV'Y 'rc'gi Va]hmci f'Ugg][ba YbhXi Y'rc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'YI hYbg]cbž'Vi hmci a i ghfYhJ]b'mci f'h]\W_Yhbi a VYf'Zfca '9I hYfbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fY'Yj UbhXcW a Ybhgt'rc]bWi XY'Ug'Yj]XYbW' 'rc'gi ddcfhmci f'Yl hYbg]cb'Udd']\WJhjcb"'\Imai 'Ya U]''9I hYfbU''Gi ddcfhmci 'k]'`Ui hca Uh]\WJ'`mfY\W']j Y'U'h]\W_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]'`'bYYX'rc'gdY\WZ\WJ'`mUg_'Zcf'cbY" Hi fb]h]b'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf"

; YbYfU`mž'UggYgga YbhitUg_g'a i ghVY'gi Va]hhYX'Y`YWfcb]WU``mj]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bghUbWfg'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'ghUhYX'cb'mci f'Wci fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYhU]`g"

@UhY 5ggYgga Ybh'DYbU`h]Yg

5b'UggYggYX'HUg_']g'XYYa YX``UhY']Z]h']g'gi Va]hhYX'UZhYf'h\Y'gdYW]Z[YX'h]a Y'UbX'XUhY'Ug'gYhci h']b'h\Y Wci fqY'@YUfb]b['A UbU[Ya YbhGmqhYa 'f@A GŁ"

$$\label{thm:condition} \begin{split} &\text{H}^{\text{U}$$

K cf_'gi Va]hhyx'zci fhyyb'fl%(EXUmg'Uzhyf'h\y'Xi Y'XUhy'k]``VY'a Uf_YX'UbX'zYYXVUW_'dfcj]XYX'Vi hbc'a Uf_ k]``VY'fYWcfXYX"'=Zh\Y'k cf_'k ci `X'\Uj Y'fYWr]j YX'U'dUgg'a Uf_'Vi hzcf'h\Y'`UhybYgg'UbX'h\Y'k cf_']g'U Wca di `gcfm'Wci fgY'Wca dcbYbhz'U'gh XYbh'k]``VY'XYYa YX'hc'\Uj Y'a Yhih\UhfYei]fYa Ybh''H\]g'XcYg'bch Udd`mhc'U'hUg_'h\Uh']g'UggYggYX'Vi hbc'a Uf_']g'Uk UfXYX"

K cf_'gi Va]hh/X'hk YbhnlcbY'f&&XUmg'UZhYf'h\Y'Xi Y'XUhY'k]```bchVY'UWWdhYX'Zcf'a Uf_]b['cf'ZYYXVUW_UbX'k]```fYWY]j Y'bc'a Uf_'cf'[fUXY"'=Zh\Y'UggYgga YbhHUg_']g'U'Wca di `gcfmWca dcbYbhcZh\Y'Wci fgY'U gh XYbhk]```Ui hca Uh]WU``mZU]`'h\Y'Wci fgY"

GdYWJU`7cbg]XYfUhJcb55dd`]WUhJcbg

 $\label{eq:linear_continuity} $$Mc_i = W_0 - W_$

G]W_bYggža]gUXj Ybhi fY'cf'ch\Yf'W]fW a ghUbWrg'VYmcbX'mci f'Wcbhfc``a Um

ł DfYj Ybhimci Zfca Wca d`Yhlb[U.Wci fqY fYei]fYa Ybhž

ł? YYd mci Zfca 'UthYbX]b['Ub 'UggYggUV`Y 'UWhj]tmž

ł Ghod moi gi Va]hh]b['UggYggUV'Y k cf_ Zcf'U Wci fgYž

ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wf`]b`UggYggUV`Y`k cf_ž`VY`]h'U`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž'U \WUgg`hYghz`U``UVcfUhcfmhYghz`U`gYa]bUf`dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa 'cZ`UggYgga Ybh'

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'\lefi\Wb'hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UVW]XYbhU`mWcdm]b['Zfca `U`gci f\W' k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidgdu[]uf]ga]bhch\YZc``ck]b[WuhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

±DUddfcdf]UhY`dUfUd\fUg]b[.'W\Ub[]b['U'ZYk'kcfXg'UbX'd\fUgYg'k\]`Y`acghmfYhJ]b]b['h\Y`cf][]bU`ghfi WhifY`UbX`]bZcfaUh]cb`k]h\ci hUW_bck`YX[YaYbh'H\]g'U`gc'Udd`]Yg`]b'dfYgYbhJh]cbg'k\YfY`gcaYcbYdUfUd\fUgYg`Ubch\Yf'g`]XYUg`cf'kcfXg'k]h\ci hWfYX]h''±iU`gc'Udd`]Yg`hc'd]YW]b['hc[Yh\Yf'ei chYg'UbXdUfUd\fUgYg`]bhc'U'bYk'k\c`Yžk]h\ci hfYZ/fYbW]b['UbX'U'ghi XYbhg'ck b'UbU`mg]g`hc'Vf]b['h\Y`aUhYf]U`hc[Yh\Yf''

7 c``i g]cb. 'k cf_]b['k]h\ 'ch\ Yfg'Vi h'dUgg]b['c\Z'h\ Y 'k cf_'Ug'U'dYfgcb'g']b\X]j]\Xi U``k cf_"'7 c``i g]cb'U`gc]b\Wi XYg'dfcj]\X]b['mci f'k cf_'hc'Ubch\ Yf'ghi XYbh\ VYZcfY'h\ Y 'Xi Y 'XUhYzcf'Zcf'h\ Y' di fdcgY'cZh\ Ya d`U[]\Uf]g]b['Uh\Ubmh]a Yz'dUm]b['Ubch\ Yf'dYfgcb'hc'dYfZcfa 'Ub'U\WUXYa]\Wh\Ug_z'ghYU']b['cf'U\\ello i]f]b[Ubch\ Yf'dYfgcb'g' U\WUXYa]\Wk cf_'Ub\X'\\ello dm]b[']hz'c\ZYf]b['hc'\\ello a d`YhY'Ubch\ Yf'dYfgcb'g' k cf_'cf'gYY_]b[d\una Ybh\Zcf'\\ello a d`Yh\beta d`

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[ˈgci fW/gˈk \]WX`\Uj Y`bchVYYb`fYUXžk]h\ci hUW_bck`YX[]b[ˈh\Y`″gYWcbXUfm″gci fW/Zfca k \]WX`_bck`YX[Y`cZh\Ya`\Ug'VYYb`cVhU]bYX"

8 i d`]\WUh]cb`ff`gY`Zld`U[]\Uf]ga "Ł`gi Va]\h]b[`mci f`ck b`k cf_ž]b`k \c`Y`cf`]b`dUfhžk \YfY`]h`\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\hYX`Zcf`Ubch\Yf`UqqYqqa Ybhcf\Wci fgY`UhI_BGK_`cf`Ubch\Yf`i b]\Yfq]\m"

7 cffYWhfYZYfYbWb[dfUWhWyg.

• VYHYfa UbU[Ymcifh]a Y

7ci fgY GWXYXi `Y

J]Yk 'WUgg'ha YHUV'Y

H]a YtUV`Y

8 UHY	Hmd Y	7 cbh/bh
K YY_'%'&*': YVfi Ufm!'(A UfWX	GYa]bUf	±blfcXi WŊcb
K YY_'&.') 'A UfWX'!'%% A UfWX	GYa]bUf	K \Uh]g:"7i `hi fY"3
		A Ulth\Yk '5fbc`Xž'gY`YWf]cbg'Zfca '5g/fgdWS` V 3`SdJZk
		F Uma cbX'K]``]Ua gž"7 i `hi fY"
K YY_" ."&"A UfWX!"% A UfWX	GYa]bUf	FYdfcXi Whjcb UbX 5 ZZjfa Uhjcb
		H\YcXcf'5Xcfbc'UbX'A Ul' <cf_\y]a 'hi="" fy<br="" yfž"7i="">=bXi glfm"</cf_\y]a>
		< YfVYfhA UfW gYž"5 ZZfa UhjjY 77 i `hi fY"
K YY_'(.'%-'A UfWX'!'&) A UfWX	GYa]bUf	GYI i U`]lm'UbX'; YbXYf
		>i X]h\ 6i hYfž"6cX]`m±bgWf]dh]cbgžDYfZcfa Uh]j Y Gi Vj Yfg]cbg"
		9jY~?cgcZg_mGYX[k]W_ž~+blfcXiW1jcb.51]caUhjW
K YY_').'&*'A UfWX'!'% 5df]`	GYa]bUf	7 f]h]ei Y
,		=a a Ubi Y``? Ubhž'"5b'5bgk Yf'hc'h\Y'E i Ygh]cb. 'fK \Uh]g'9b`][\hYba Ybh3fi
		A]WWY`: ci WUi `hž'"K \Uh`]g'7f]h]ei Y3"
		6fi bc'@Uhci fž'"K \m< Ug'7f]hjei Y'Fi b'Ci hcZ GhYUa 3': fca 'A UhhYfg'cZ: UWhhc'A UhhYfg'cZ 7cbWYfb"
K YY_'*.'-'5df]`'!'%)'5df]`	GYa]bUf	7i `hi fY'Bck
		GY`YW¶cbgʻZfca 'HYffm9U[`Yhcbž5g′fgdW
		7]micZGmXbYmž5dWSf[hW5 [fk, 5g/fgdS^Ba/fUk S`V 3Uf[a`B/S`\$"#&Ž\$"\$&
		7]micZGmXbYmž5[fk 3df, BgT1[U 3df E fdSfWYk

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

H\YcXcf`5Xcfbc`UbX`A UI`<cf_\Y]a Yfž"7i`h fY`±bXi ghfm³ž`]b`FZW6 [S^WJf[UaX7` {YZfW_ W fz'hfUbg" 9Xa i bX`>Yd\WchnfGhJbZcfX`I b]j Yfg]lmiDfYgglž'dd"-(!% *"

A Uth\Yk '5fbc`Xž'5g'fgdWS` V 3` SdJZkž'YX"'GtYZJb'7c``]b]'fl7 Ua Vf]X[Y'l b]j Yfg]tmiDfYggž'% - ' Łž'dd") ' !\%) "

>i X]h\ '6i hYfz''6cX]`m'±bgWf]dh]cbgž'DYfZcfa Uhjj Y'Gi Vj Yfg]cbg''ž']b'9W VWdFdagT WfBYk 'Mcf_, 'F ci hYX[Yž%---Łž'dd"'%*'!%\$"

7]micZGmXbYmž5[fk 3df, BgT/[U 3df E fdSfW/k"

7]micZGmXbYmž

7 F *=*7 C G

7F=7CG'Dfcj]XYf'7cXY.'\$\$\$-,;