

MDIA2011

A YX]U 8 Yg][b Zcf 7 \ Ub[Y

GYa YghYf'C bY''##'&\$%

7ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g`

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
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GWkcc~7cbhJWh~abZcfa Uh]cb

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D\cbY. f\$&L'-',) '(,) *

9a U]`.'gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.##qUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'thY'HfUX]tjcbU``7i gtcX]Ubgž thY'6YXY[U'`fPYbg]b[tcb'WJadi gtž; UX][U'`fP]tmUbX'5fth' '8Yg][b'7Uadi gYgt'UbX'thY'B[i bbUkU' dYcd'Y'fbi gtfU']Ub'8YZYbW': cfW'5WJXYam']b'7UbVYffUt'cZthY'`UbXg'k\YfY'YUWX'WJadi g'cZl BGK ']g`cWJtYX''$

5 hhyb XUb WY F Yei]fYa Ybhg

5 'ghi XYbhi]g'Yl dYWYX'hc'UhrYbX'U```WUgg'WebhUWi\ci fg'Zcf'U'ZUWY!hc!ZUWY'fl &: Ł'cf'V`YbXYX'Wei fgY'UbX Wea d'YhY'U```UWIjj]hjYg'Zcf'U'VYbXYX'cf'Z ``mcb`]bY'Wei fgY"

5 'ghi XYbhik \c'Uff]j Ygʻa cfY'h\ub'%) 'a]bi hYgʻ`UhY`a UmVY'dYbU`]gYX'Zcf'bcb!UhhYbXUbWY'''⊋gi W\'U'dYbU`hm

: cf`YggYbhJU``ghi XYbh`]bZcfa UhJcb`fY`UhJb[`hc.`fYei Yghg`Zcf`YI hYbg]cb/fYj]Yk `cZa Uf_g/cWW dUhJcbU``\YU`h\UbX`gUZ/hm/YI Ua]bUhJcb'dfcWXi fYg/gdYWJU``Wcbg]XYfUhJcb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybhi fY/ghi XYbhYei]hm'UbX`X]gUV]`]hm'UbX`ch\Yf`YggYbhJU``UWUXYa]W]bZcfa UhJcbž gYY`\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhghi XYbhg#UWUXYa]W]bZcfa UhJcb#dfchcWc`g![i]XY`]bYg#

7 ci fgY 8 YHJ] g 7 fYX]hDc]bhg * Gi a a UfmcZh\Y 7 ci fgY

EgTWUf3dWS. AYX]U

#Dith]giWci fgYzimci ik]```XYj Y`cdigdYW]U`]gh_bck `YX[Yicbih\Yii gYicZh\Yia YX]U'Zcfi]bhYfbUhJcbU`
XYj Y`cda Ybhk cf_"'H\fci [\ih\YiXYg][bicZu'a YX]U'dfcYWhHJf[Yh]b[i]ggi Ygih\UhUZZYWhh\Yi`]j YgicZdYcd`Y
]bigca YicZh\Yia cghX]gUXj UbhU[YX'UfYUgicZh\Yik cfiXzimci ik]```YUfbi\ck ibciWfYUhYia YX]U'ghfUhY[]Ygih\Uh
dfca chYidcg]hjj YiVY\Uj]ci fiUbXigcW]U`W\Ub[YziUbXik\]W\Wbbii hja UhYimhfUbgZcfa idYcd`Yfgii]j Yg"K\]Y
h\YfYi]giUbiYa d\Ug]gibcXUmcbih\Yii gYicZgcW]U`a YX]U'UbXi]bbcj Uhjj YihYW\bc`c[]YgibciUXj cWUhYiW\Ub[Yzi]bih\]giWci fgYik YiUfYifYa]bXYXih\UhWca a i b]WUhjcbiW\UbbY`gij Ufmcbih\YiVUg]gicZU'Wci bhfmfgiYWcbca]W
UbXigcW]U`WcbhYI hia cfYcj YfziX]ZYfYbWYgi]biYh\b]WVUW_[fci bXziUb[i U[Yzi[YbXYfziYj Y`cZi]hYfUWhUbX
i fVUbihcifi fU`gYhh]b[giUfYiWfi W]U'ij Uf]UVYgik\Ybik Y`cc_"UhXYj Y`cda YbhWcbhYI hg"iH\fci [\ih\]giWci fgYz
mci ik]``k cf_hck UfXgiU'WYUh]j Yii gYicZVch\bYk UbXifUX]hjcbU`a YX]U'd`UhZcfa gihc'UW\]yj Yiw\Ub[Y"

5 hm Y WcbWi g]cb cZm]g Wci fgY h Y gh XYbhk] ` VY UV Y hc

- %" 8]gW gg 'UddfcUW.Yg 'fc 'a YX]U ']b ']bhYfbUh]cbU``XYj Y`cda Ybhk cf_ 'UbX 'YI d`U]b 'fY`Yj Ubhh\YcfYh]WU` UbX 'WcbW'dh U``ZfUa Yk cf_g 'Zcf`XYj Y`cda YbhUbX 'gcW]U` 'W. Ub[Y"
- &" 9j U`i UHY'H\Y'fc`Y'cZH\Y'a YX]U'UbX'a YX]U'dfUW{WY']b'XYj Y`cd]b['WcbHYI hg"
- ʻ"8Yg][b'U'fYgYUfW\'d`Ub'Zcf'h\Y'dfcXiWhjcb'cZW'hifU`` JUUX '\$**%, %**! fmfb

5ggYgga Ybh

 $D^YUgY'i gY' < Ufj UfX'F YZYfYbW]b['GhmY'Zcf'U```UggYgga Ybhg''`5'ei]W_[i]XY'hc'h\Y'i gY'cZh\]g'ghmY'WUb'VY Zci bX'\YfY.''$

\hdg.#k k k "X]h']Y#a YX]U#]VfUfm#XcWa Ybhg#8 +Hi &\$@]VfUfm &\$< Ufj UfXi &\$E i]W i &\$; i]XY"dXZ

5 'gi a a UfmcZh\Y'UggYgga YbhUbX'i gYZ\``fYgci fW'g'Zcf'h\]g'Wci fgY'WUb'U`gc'VY'Zci bX`]b'h\Y'5ggYgga Ybh XcW a Ybhcb'A ccX`Y"

5ggYgga Ybh'HUg_g'

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UhY	Gh XYbh@YUfb]b[CihWca Ygʻ5ggYggYX
@hYfUhi fY`fYj]Yk`	' \$1	&) #\$' #&\$% `\$, .\$\$`DA	%ž&
A YX]U'dfc YWhd`Ub') \$1	\$*#\$) #&\$% `\$, .\$\$`DA	&Ž
J]XYc'dfYgYblUlf]cb'	&\$ı	Hi hcf]U`g`K YY_`%	&ž(

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh'% @]hYfUh fY fYj]Yk

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. %) \$\$ k cfXg

 $8YHU]^*g. \% $\$^k \ cfXg''H^]g^*]g^*h^Y^*Z]^fgh^UggYgga \ Ybh^HUg_'': \ YYXVUW_k \]^*VY^*dfcj \]XYX^]b^k \ f]^HYb^*Zcfa ^UbX bi a \ Yf]^WU^*[\ fUXY''']$

5XX]h]cbU`XYhJ]`g.

±0.1h\]g'%) \$\$!k cfX YggUmžmci 'k]``cZYf'Ub'cj Yfj]Yk 'cZh\Y'`]hYfUhi fY']b'h\Y'Z]Y`X'cZa YX]U'Zcf'XYj Y`cda Ybhž 'cc_]b['Uh'VY\Uj]ci f'W\Ub[Y'h\Ycf]YgžgcW]U``a Uf_Yh]b[žgcW]U``W\Ub[YžYXi hU]ba YbhžWca a i b]hm'UbX dUfh]W]dUhcfma YX]U"'H\Y'WcbhYbhicZmci f'YggUmk]``fYj c'j Y'Ufci bX'h\Y'h]hY'cZ'A YX]U'Zcf'8Yj Y`cda Ybh h\Ycfm!Xf]j Yb'UddfcUW\Yg']b'i g]b['h\Y'a YX]U'Zcf'W\Ub[Y'"'Hc'dfcXi WY'h\]g'k cf_žmci 'g\ci `X'i h]`]gY'U a]b]a i a 'cZ, 'UWUXYa]Wgci fWYg"

5ggYgga Ybh& A YX]U'dfc YWhd`Ub

GHUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. %) \$\$ k cfXq

8YHJ]`q. '&) \$\$`k cfXq": YYXVUW_k]```VY`dfcj]XYX`]b`k f]HYb`Zcfa `UbX`bi a Yf]WU``[fUXY"``

5XX]h]cbU`XYhU]`g.

± 'h\]g'&) \$\$!k cfX`fYdcfhz`mci 'k]```dfYgYbhimci f'a YX]U'dfc YWid`Ub`UbX`X]gWi gg'h\ Y`ghYdg'hU_Yb'hck UfXg']hg XYg][b"

cf'h\Y'dfcYVfiXYg][bžmci k]``VY'dfcj]XYX'k]h\'U'W\c]W'cZ) 'X]ZZYfYbha YX]U'dfcYVfigWbUf]cg'fY`UhYX'hcX]ZZYfYbhXYjY`cdaYbh]ggiYg']b'gdYWZ]WWcibhf]Yg'cZh\Y'; `cVU``Gcih\"'6UgYX'cb'h\Y'gWbUf]c'cZmcif W\c]WYžmci k]``kcf_k]h\'ch\Yf'ghiXYbhg'cb'h\Y'Zc``ck]b['UWf]j]h]Yg'Xif]b['hh hcf]U'g.

%" gYM]b[WYUfcVYW] Yg Zcfh\Y a YX]U dfcYWY

- &" XYg][b]b['U'fYgYUfV\\'d`Ub'hc'[Uh\Yf']b\Zcfa Uh]cb'cb'h\Y']ggi Y'h\Y'a YX]U'dfc'Y\Wik Ubhg'hc'UXXfYggž]b\Wi X]b['df]a UfmfYgYUfV\\'a Yh\cXgz'dcdi `Uh]cbz'UbX'gUa d`Y'gY`Y\W]cb/
- ' " WcbXi Wgb['XYg_fYgYUfW\cb'h\Y']ggi Y'h\Y'WJa dU][b']g'ffm]b['hc'UXXfYggžk]h\dUffjW`Uf'UffYbf]cbdu]X'hc'W'hi fU'žfY`][]ci g'UbX'ffUX]hcbu``gYff]b[g/
- ("fYgYUfWX]b["h\Ya YX]U"UbXgWUdYcZh\Y'Wci bhfmh\Ya YX]U'dfcYWhk]``VY']a d'Ya YbhYX']b/
-) " fYgYUfWX]b['UbX']XYbfjZm]b['YZZYWfj Y'a YX]U'WXUbbY`g'cb'f\Y'VUg]g'cZf\Y'W\`hi fU`ž'dc`]fjWU``UbX hYWXbc`c[]WU``fYU`]hmcZh\Y'Wci blfm/
- *"]XYbh]Zm]b['Uddfcdf]UhY'a YggU[Yg'hc'fYUWX'hXY'hUf[YhUi X]YbWY/
- +" XYj Y`cd]b['WYUf']XYUg'cb'UbX'X]gW gg]b[']b'XYhU]`g'h\Y'a YX]U'ci hdi hg'hc'VY'WfYUhYX'Zcf'h\Y dfc'YVW
- , "cih]b]b['U'd'Ub'Zcf'a cb]hcf]b['UbX'Yj U'i Uh]cb"

9 UWX 'ghi XYbhik]``'h\Yb'dfYdUfY'Ub']bX]j]Xi U`'k f]hhYb'Wca dcbYbh#gYWf]cb'cZh\Y'a YX]U'd`Ubžk \]W\'k]``'VY gi Va]hhYX'Ug'cbY'Wc\Yg]j Y'XcW'a Ybh''NCi 'k]``'VY'a Uf_YX'cb'h\Y'gYWf]cb'cZh\Y'd`Ub'mci '\Uj Y'dfcXi W'Xž UbX'cb']hg'fY`Yj UbW''hc'UbX'Wc\YfYbW''k]h\'h\Y'fYghcZh\Y'd`Ub''

 $\label{eq:higher} \mbox{Hi fb]h]b"gYh]b[."H\]g"Ugg][ba Ybh]g"gi Va]hhYX"h\fci [\ \ 'Hi fb]h]b"UbX"gh XYbhg"Xc"bchgYY"Hi fb]h]b q]a]`Uf]hmfYdcfhg"$

5ggYgga Ybh' . 'J]XYc dfYgYbhUh]cb

GHJfhXUhY. Bch5dd`\WJV`Y

@Yb[h\. (a]bihygf]Uf]UVYVUgYXcb[fcidg]nYŁ

8 YHU]`g. ; fci d'dfYgYbHuh]cb'f]b'j]XYc'Zcfa UHzcZ(!) 'ghi XYbhg"'H\Y'fYei]fYX``Yb[h\'cZh\Y'j]XYc']g'U a UI]a i a 'cZ('a]bi hYg"H\]g']g'h\Y'Z]bU`'UggYgga Ybh'HUg_'Zcf'UhhYbXUbWY'di fdcgYg": YYXVUW_'k]``'VY dfcj]XYX']b'k f]hhYb'Zcfa 'UbX'bi a Yf]WU`'[fUXY'Ug'U'[fci d'a Uf_"''

5XX]h]cbU`XYhU]`g.

9UW. [fci dˈk]```gi Va]hʿU`('a]bi hY``cb['j]XYc'dfYgYbhJhjcb'fXYdYbX]b['cb'h\Y'g]nY'cZh\Y'[fci dłž]``i ghfUhjb['h\Y`XYg][b'cZcbY'a YX]U'ci hdi hih\Uhik Ug']bWi XYX']b'h\Y]f'dfc'YWid`Ub"'Ghi XYbhg'WJb'i gY'ghj``]a U[Ygž'Ub]a Uhjcb'UbX'i]XYc'ZcchJ[Yž'cf'U'Wca V]bUhjcb'cZh\YgYž'UbX'dfYdUfY'U'bUffUhjcb'Ug'Ui X]c

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

 $Gh\ XYbhg\ UfY\ YI\ dYWMYX\ hc\ di\ hih\ Y]f\ bUa\ Yg\ UbX\ gh\ XYbhbi\ a\ VYfg\ cb\ Yj\ YfmdU[\ Y\ cZh\ Y]f\ Ugg][\ ba\ Ybhg\ bug\ Ybhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\$

Hi fb]h]b Gi Va]gg]cb

⊋mci 'YbWci bhYf'U'dfcV'Ya 'k \Yb'UhhYa dhjb['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]hjbž'd'YUgY hY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-' ,) '' ' '%cf'Ya U]'hXYa 'cb'<u>Yl hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui</u> ł `G][b]Z]\WbhmUZZY\Wimci f`dYfZcfa Ub\Wi]b`UggYggUV`Y`k cf_ž`VY`]hU`Zcfa U``YbX!cZgYa YghYf`Yl Ua]bUh]cbž'U`\WUgg`hYghž'U``UVcfUhcfmihYghž'U`gYa]bUf'dfYgYbhUh]cb`cf`Ubmch\Yf`Zcfa `cZ`UggYgga Ybh'

: cf'Z fh\Yf'XYhJ]`g']b'fY`Uhjcb'hc'GdYWJU`'7 cbg]XYfUhjcb']bWj]&J|b['''K \Yb'hc'5dd`m'ž''<ck'hc'5dd`m''UbX''Gi ddcfhjb['8cW'a YbhUhjcb''d`YUgY'fYZYf'hc'h\Y'GdYWJU`'7 cbg]XYfUhjcb'k YVghJY.'\hdg.#gh'XYbh'i bgk "YXi "Ui #gdYWJU`!Wcbg]XYfUhjcb

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i\in\WbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiW\YUh]b[ihciUVW]XYbhU`mWcdm]b[iZfca iUigci fWlik]h\ci hiUW_bck iYX[Ya Ybh'i

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b[`WUhY[cf]Yg.$

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`h\I hcf']XYU'k]h\ci hUW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U'gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]hY[cf]Yg.

- VYMYfa UbU[Ymcifh]a Y
- i bXYfgHUbX mci f'f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'UhI BGK
 VY`Uk UfY`cZd`U[]Uf]ga žWcdmf][\hz`I BGK 'Gh XYbh'7 cXY`cZ7 cbXi Wh'UbX`5VWWdhUV`Y`I gY`cZ IBGK '=7 H'F Ygci fWYg'Dc`]Wm

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

B#5

FYWca a YbXYX FYgci fWYg

D`YUgY`j]Yk 'h\Y`5ggYgga YbhXcW a Ybhcb'A ccX`Y"

7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

±JZcfa U``ZYYXVUW_`cb`h\Y`Wci fgY`k]```VY`gci [\hih\fci [\`Ub`]b!WUgg`ei Ygh]cbbU]fY`Xi f]b[`h\Y`Wci fgY`cZh\Y`gYa YghYf"

: cf²Z|bU`Wci fgY`Yj U`i Uh]cbžghi XYbhg`k]``fYVW]j Y`U``]b_'hc`h\Y`A m9I dYf]YbWY`gi fj Ymihck UfXg`h\Y`YbX`cZ h\Y`gYa YghYf"

=a U[Y 7 fYX]h

6cX]Yg'/ *\D\YfZJ\W\g'\&\\$*

7F = 7CG

7F = CG'Dfcj]XYf'7cXY.\$\$\$-,;