

MDIA5003

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5 'ghi XYbh']g'Yl dYWYX'hc'UhhYbX'U```WUgg'WcbhUWi\ci fg'Zcf'U'ZJWY!hc!ZJWY'fl &: Ł'cf'V`YbXYX'Wci fgY'UbX Wca d`YhY'U```UWIji]hiYg'Zcf'U'V`YbXYX'cf'Z ``mcb`]bY'Wci fgY"

5 'ghi XYbhik \c'Uff]j Yg'a cfY'h\Ub'%) 'a]bi hYg'``UhY'a UmVY'dYbU`]gYX'Zcf'bcb!UhhYbXUbWY'''=Zgi W\'U'dYbU`hm]g']a dcgYXž'h\Y'ghi XYbha i ghiVY']bZcfa YX'j YfVU``mUhih\Y'YbX'cZWUgg'UbX'UXj]gYX']b'k f]h]b['k]h\]b'&(\ci fg"

⊒Uʻghi XYbhYl dYf]YbWrgʻ]`bYggža]gUXj Ybhi fYʻcfʻch\YfʻcWW ff\bWrʻh\Uha U_YgʻUVgYbWʻʻZfca ʻU WUgg#UWfj]hmi bUj c]XUV`YžcfʻYl dYWgʻhcʻVYʻUVgYbhZfca ʻUʻZcfh\Wca]b[ˈWUgg#UWfj]hmžh\Ymg\ci `XʻgYY_ dYfa]gg]cbʻZfca ʻh\Yʻ7 ci fgYʻ5i h\cf]hmžʻUbXʻk \YfYʻUdd`]WUV`Yžh\Y]fʻfYei Yghg\ci `X'VYʻUVWca dUb]YXʻVmUb cf][]bUʻʻcfʻVWffjZJYX`WcdmcZUʻa YX]WUʻ`WYffjZJWUhYʻcfʻch\YfʻZcfa ʻcZUddfcdf]UhYʻYj]XYbWY"

5 '7 ci fgY '5 i h\cf]hma UmYI W gY 'U'ghi XYbhZca 'WUggYg'cf'UWfj]hJYg'Zcf'i d'hc'cbY'a cbh\" < ck Yj Yfz'h\Ym a UmUgg][b'UXX]hJcbU``UbX#cf'U'hYfbUhJ Y'HUg_g'hc'Ybgi fY 'Wca d`]UbW\" '5 '7 ci fgY '5 i h\cf]hmWcbg]XYf]b['th\Y [fUbhJb['cZUVgYbW'a i ghVY'gUfJgZ]YX'U'ghi XYbhk]```ghJ```VY'UV'Y'hc'a YYhh\Y'Wci fgY'g'`YUfb]b['ci hWca Yg UbX#cf'j c'i a Y'cZ`YUfb]b["'5 'ghi XYbhgYY_]b['Uddfcj U``hc'VY'UVgYbhZcf'a cfY'h\Ub'cbY'a cbh\'a i ghUdd`m]b'k f]hJb['hc'h\Y'8YUb'UbX'dfcj]XY'U``cf][]bU``cf'Wff]ZYX'gi ddcfhJb['XcW a YbhUhJcb"

: cf'a cfY']bZcfa Uhjcb'UVci hih\Y'UhhYbXUbWY'dfchcWc`g']b'h\Y': UWY`hmicZ'5fhg'UbX'GcWjU`GWjYbWYg.'\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbh!ghi XYbhg#UWUXYa]W]bZcfa Uhjcb#dfchcWc`g![i]XY`]bYg#

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: cf`YggYbh]U``ghi XYbh`]bZcfa Uh]cb`fY`Uh]b[`hc.`fYei Yghg`Zcf`Yl hYbg]cb/fYj]Yk `cZa Uf_g/cWW dUh]cbU``\YU`h\UbX`gUZ/hm'Yl Ua]bUh]cb`dfcWXi fYg/gdYW]U``Wcbg]XYfUh]cb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybhi fY/ghi XYbhYei]hmUbX`X]gUV]`]hm'UbX`ch\Yf`YggYbh]U``UWUXYa]W]bZcfa Uh]cbž gYY`\hdg.#k k k "Ufhq"i bqk "YXi "Ui #W ffYbhqhi XYbhq#UWUXYa]W]bZcfa Uh]cb#dfchcWc`q![i]XY`]bYq#

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D`YUgY`fYZYf`hc`XYhU]`YX`[i]XY`]bYg`UbX`gi ddcfhfYgci fWYg`cb`A ccX`Y"

 $\label{thm:limit} \begin{tabular}{ll} Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h "UbX"h Xybhg"Xc "bchgYY"Hi fb]h "UbX"Hi fb]h "UbX"h Xybhg"Xc "bchgYY hy Xybhg"Xc "bchgY$

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 $Gh\ XYbhg\ UfY\ YI\ dYWMYX\ hc\ di\ hih\ Y]f\ bUa\ Yg\ UbX\ gh\ XYbhbi\ a\ VYfg\ cb\ Yj\ YfmdU[\ Y\ cZh\ Y]f\ Ugg][\ ba\ Ybhg\ bug\ Ybhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ bug\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\ Yhhg\ bug\ Yhhg\ Yhhg\$

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: cf'Z fth\Yf'XYfU]'g']b'fY`Ufjcb'fc'GdYWJU`'7 cbg]XYfUfjcb']bWj]XJJb[''"K \Yb'fc''5dd`m"ž'"<ck'fc''5dd`m"'UbX "Gi ddcftjb['8cW a YbfUfjcb'''d`YUgY'fYZYf'fc'th\Y'GdYWJU`'7 cbg]XYfUfjcb'k YVgfjY.'\htdg.#ghi XYbf'i bgk "YXi "Ui #gdYWJU`!Wcbg]XYfUfjcb

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7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`h\I hcf']XYU'k]h\ci hUW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U'gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]hY[cf]Yg.

- VYMYfa UbU[Ymcifh]a Y
- i bXYfgHUbX mci f'f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'UhI BGK
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