



ARTS3021

7 fYUhjj Y'K f]hjb['=bhYfbg\]d

HYfa 'C bY''##'&\$%-

7ci fgY'Cj Yfj]Yk

Ghuzz 7 cbhuWh8 Yhu]`g

'7cbj Ybcfg'

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GWkcc~7cbhJWh~abZcfa Uh]cb

Fcca " &ž`Yj Y`" FcVYfhK YVghYf`6i]`X]b[

D\cbY.'f\$&E'-',)'(,)*

9a U]` gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.#gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7i gtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[tcb'WJa di g\cong tz'; UX][U'`fP]tmUbX'5fth/ '8Yg][b'7Ua di gYg\cong tubX't\Y'B[i bbUk U` dYcd'Y'fbi gtfU']Ub'8YZYbW': cf\w'5\\WXYa m']b'7UbVYffU\cozh\Y'`UbXg'k\YfY'YUW\cozh\Y'YUW\cozh\Y''UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'''\UbXg'k\YfY'YUW\cozh\Y''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'' \cozh\Y''' \cozh\Y''$

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7 fYX]hDc]bhg *

Gi a a UfmcZh\Y 7ci fgY

GiVYWh5fYU.5dWSf[hWId[f[`Y'

H\]g`Wci fgY`dfcj]XYg`mci `k]h\`Ub`cddcfi b]lmirc`i bXYffU_Y`k cf_!]bhY[fUhYX``YUfb]b[`UbX`[U]b`]bXi glfm YI dYf]YbW' k]h\`U`\cghcf[Ub]gUh]cb`WcgY`mfY`UhYX`hc`mci f`A U`cf`]b`7 fYUh]j Y`K f]h]b["`Mci `a Um'U`gc`Udd`m hc`k cf_`cb`UhHUW\a Ybhcb`Ub`UWUXYa]WfYgYUfW\`dfc`YWicf`k cf_`]b`Ub`YX]hcf]U``fc`Y`Zcf`Ub`UWUXYa]W 'ci fbU`"`\\YU``mž'mci `k]``i bXYffU_Y`Ub`]bhYfbg\]d`UZhYf`mci `\Uj Y`Wca d`YhYX`%') `mYUfg`cZZ\``!h]a Y`ghi Xmfcf Yei]j U`YbhL'UbX`Wca d`YhYX`U`a]b]a i a `cZ%\ `I C 7 `]b`h\Y`A U`cf"`5hih\Y`YbX`cZh\Y`]bhYfbg\]d`"cfcj]XY`U`gi a a Uh]j Y`fYdcfhcZmci f`YI dYf]YbWYg`UbX`k cf_`YI Ua d`Yg`Wca d`YhYX`Xi f]b['h\Y`]bhYfbg\]d"

H\Y']bhYfbg\]d'fYei]fYg'U'rchU``Wca a]ha YbhcZ%\$\$!%) \$`\ci fg'cZk cf_'k]h\'U'\cghcf[Ub]gUh]cb'UbX'a Um bcfa U``m'VY'hU_Yb']b'Z]fghžgYWcbX'cf'gi a a Yf'gYa YghYf'' =bhYfbg\]d'cddcfhi b]h]Yg'UfY'UXj Yfh]gYX'j]U'h\Y GW\cc``cZh\Y'5fhg'UbX'A YX]U' =bhYfbg\]d'BYk g'YhYf''5'hYfbUh]j Y`mmci 'a UmUddfcUW\'U'fY'Yj Ubh cf[Ub]gUh]cb'hc'Udd`mZcf'Ub']bhYfbg\]d'''Df]cf'hc'gYY_]b['Ub']bhYfbg\]dz'mci 'g\ci `X'UhYbX'Ub']bhYfbg\]d]bZcfa Uh]cb'gYgg]cb'fi b'Vmh\Y'GW\cc``cZh\Y'5fhg'UbX'A YX]U''

Hc VY Y`][]V`Y Zcf'h\]g Wci fgYzmci a i gh\Uj Y U a]b]a i a 'K 5A 'cZ+\$"

7 ci fgY @YUfb]b['Ci hWca Yg

%" \Uj Y`[U]bYX`YI dYf]YbW`cZ]bXi ghfmdfc\WggYg`UbX`dfU\Wj\Wg &" Udd`mh\YcfYhj\Wb``Wcb\Wdhg`UbX`dfU\Wj\\Wb``g_]``g`[U]bYX`]b`h\Y`dfc[fUa `hc`fYU`!k cfX`\\chi\Y hg \\ ' " \Uj Y`Yb\Ub\\X'h\Y]f`\\Ud\\Jhm\Zcf`]bXYdYbXYbhYb[U[Ya Ybhk]h\`]bXi ghfmdfcj]XYfg

HYUW]b['GhfUhY[]Yg'

 $H\]g'Wci\ fgY'\ Ug'bc'Zcfa\ U`'hYUW\]b[\ 'Wca\ dcbYbh'''$

5ggYgga Ybh

7 ci fgY fYei]fYa Ybhg]bWl XY.

- 7 ca d'Yhcb'cZU'a]b]a i a 'cZ%\$\$'\ci fg'cZd'UWYa Ybh
- Gi Va]gg]cbg'cZUggYgga Ybh'lUg_g'%/ '&'XYa cbglfUl]b['U'gYf]ci g'UlthYa dhihc'Ubgk Yf'l\Y'lUg_fYei]fYa Ybhg
- Gi Va]gg]cb cZVch\ h\Y \cghUbX gh XYbhZYYXVUW_ Zcfa g

5ggYgga YbhHUg_g

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7 f]h]WU`F YZYWn]cb') \$1	5bmifja Y'VYZcfY') da 'cb'fh\Y : f]XUmcZK YY_'%\$"	%ž&
K cf_'9j]XYbW') \$1	5bmilja Y VYZcfY) da cb l\Y : f]XUmcZK YY_'%\$"	%1

5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% 7f]hJWU`FYZYWhJcb

GhUfh XUhY.

 $8 YHJ]^*g. "Gh XYbhg"k]^*"gi Va]hU'Wf]hJWU'`fYZYWf]cb"k \] WXVf]YZmXYgWf]VYg"hXY'hmdY"cZcf[Ub]nUh]cb"hXYmik YfYdUWYX"]b"UbX"hXY]f"fc"Y k]hXJbUW bUW'$

XYgWf]dh]cb'cZk cf_Zck']b'fY`Uh]cb'hc'U'`Uf[Yf'dfcWfggžcf'g]a]`Ufž']Y']hg\ci`X'dfcj]XY'Yj]XYbWf'cZdfUWf]WU`k cf_'i bXYfhU_Yb'Xi f]b['h\Y'd`UWfa Ybh''H\]g'g\ci`X'VY'U'a]b]a i a 'cZ&)\$'k cfXg'Vi ha Uma U_Y'i d'a cfY cZh\Y'Wca V]bYX'hchU''cZ%)\$\$!&)\$\$'k cfXg'Zcf'Vch\'UggYgga Ybh'Wca dcbYbhg"; fUX]b['k]``VY GUh]gZUWcfm# bgUh]gZUWcfmUbX'gca Y'gi a a Uh]j Y'ZYYXVUW_'k]``VY'dfcj]XYX"

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

 $H\YfY\UfY\bc\dfYgWf]VYX\fYgci\fWYg\Zcf\h\]g\Wci\fgY"$

FYWca a YbXYX FYgci fWYg

7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

@f]YZmci h]bY`\ck 'ghi XYbhZYYXVUW_flVch\ 'Zcfa U``UbX`]bZcfa U`E'cb'h\Y`Wci fgY`k]```VY`[Uh\YfYXž\ck ']h k]```VY`UbU`mgYX`UbX`\ck ']hk]```VY`UbWYX`i dcb'hc']a dfcj Y`h\Y`ghi XYbh`YUfb]b['YI dYf]YbWY": cf'YI Ua d`Yž mci 'a][\hX]gW gg`k \Uhk Ug`]XYbh]Z]YX`]b'dUghZYYXVUW_UbX`\ck 'h\]g`Wci fgY`k Ug`W\Ub[YX`hc`UXXfYgg`h\Y]ggi Y"Q

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

_Zmci YbWci bhYf'U'dfcV`Ya 'k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]hJbž'd`YUgY
hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'' =Zmci
UfY'i bUV`Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZUi 'hk]h\'Hi fb]hJb'mci 'a Um'Udd'mZcf'Ub'Y! hYbg]cbžVi hmci
a i ghfYhU]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU``Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'' =Zmci 'Ya U]`'9! hYfbU``Gi ddcfhmci 'k]``

5 WUXYa | W < cbYghmUbX D`U[| Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_]b['k]th 'cth Yfg'Vi hidUgg]b['cZZth Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY