

# **ARTS3022**

BUffUhjj Y. H\Y 5 fh UbX GWYbWY cZGhcfmhY``]b[

HYfa 'C bY''##'&\$%-

# 7ci fgY<sup>-</sup>Cj Yfj ]Yk

# 'GhJZZ'7cbhJWh'8YhJ]`g'

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWJhjcb	D\cbY
5ggcWJUHY DfcZYggcf DUi`8Ukgcb	dUi `"XUk gcb4 i bgk "YXi "Ui	,	fa '&% ž`Yj Y` &ž'K YVghYf 6i]`X]b[	- ' , ) &&&\$

### GWXcc~7cbHJWh~\partialZcfa Uh]cb

 $\label{eq:final_problem} F\ cca\ ''\ \&\&\check{z}``Yj\ Y``'\ `F\ cVYfh'K\ YVghYf`6i\ ]`X]b[$ 

D\cbY. f\$&Ł'-',) '(,) \*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.#gUa "Ufhg"i bgk "YXi "Ui

H\Y**% %** `cZfH\Y UffmbY`A "YV]"gcUi Xž`]\_\Y c' `ZYdZUWZUi `6m5U\_Ybk ``X[\Y H\Y UUYWUf]cUc``i VgcYWJi

# 7ci fgY 8YHJ] g

7 fYX]hDc]bhg \*

Gi a a UfmcZh\Y 7ci fgY

GiVYWh5fYU.5dWSf[hWI d[f[`Y

H\]g'Wci fgY'WUb'U`gc'VY'ghi X]YX']b'h\Y'Zc``ck ]b[ 'gdYW]U`]gUh]cb.'7` Y{eZ

 $H\[g] \wci fgY \xyj Y \cdg'mci f'g_] \grib f] [\cfci g' \wcgY' fYUX] b[\czh\ Y' \Zcfa U' Y' Ya Ybhg' \cZbUffUhjj Y' Z] \wf] cbz YbUV \] b[\cmci hc' \VYhhYf'i bxYfgHUbx' Ubx' UddfY W] UhY' \ck' Z] \wf] cb'k cf_g''' K \Uh'] g' U' bUffUhjj Y 3'8 c' U' bUffUhjj Y 3'8 c' U' buffUhjj Y 3'8 c' U' \Zv Uhi fYg3' < ck' Xc' Ui h\cfg' \wbghfi \wh\\Y] f' ghcf] Yg3' < ck' Xc' fYUXY fg' fY\wc[b] nY' Ubx a U_Y' gYbgY' cZh\YgY' ghcf] Yg3' \wci 'k ]''' YUfb' h\Y' df] bW] d' Yg' cZbUffUhc c[mz' Ubx' \ck' ] hdfcj ] \xYg' U' dcYh] \wg' cZ \Z\wf] cF' \wf] h\wg' Ubx' k f] hYfg'' \wci 'k ]''' YUfb' h\Y' df] bw] d' Yg' cZbUffUhc c[mz' Ubx' \ck' ] hdfcj ] \xYg' U' dcYh] \wg' cZ \Z\wf] b\x Tyg' U' dcYh] \wg' \xZf\wf] bx] fY\wh \x\] g\wci fgYz' dYfgdY\wf] Yz'i bfY' \] Uv'Y' bUffUhj cbz' Ubx' h\Y' dUfUhYI h' 5' bi a \xYf' cZfY\wf bhh\ YcfYh] \wf' \xUddfc U\xXyg \nc bUffUhj Y' fZYa \] \b] g\nz' \wci [\b] hj Yz'f\Yhcf] \wf' \x' Y' di h'] \bnc \x\] U'c[i Y' k] \h\ YU\x\ ch\Yf' Ubx' Ya d' cmYx' \nc UbUhca \] \ny bcj Y'g' h\Uh'\Uj Y' dfcj c_Yx' \wcbhfcj Yfgmcf' Yh\] \wf' \xxy\VUhYg' Ua cb[ghfYUXYfg'' \]$ 

### 7ci fgY @YUfb]b[ Ci hWca Yg

%" ⇒XYbh]ZmUbX'YI d`U]b'h\Y'Zcfa U`ZYUh fYg'cZbUffUh] Y'Z|W|cb

- &" 5bU`my`h\y`fy`Uhcbq\]d`VYkk YYb`Zcfa`'UbX'WcbhYbh]b`]bX]j [Xi U``k cf\_g`cZbUffUhj Y`Z|Whcb
- ' " =6HYffc[UHY'H\Y'fY`UH]cbg\]d'VYHk YYb'H\YcfYH]WU``WcbWYdhg'UbX'Wf]H]WU`#WfYUH]j Y'dfUWf]WY
- ("5ggYgg'h\Y'a U'cf'a cj Ya Ybhg'UbX'a Yh\cXc'c[]\W\'XYVUhYg'k]h\]b'bUffUh]j Y'h\Ycfm

### HYUWX]b[ 'GhfUhY[]Yg'

#### HYUW ]b[ ghfUhY[ ]Yg

Œ````YWhi fYg`hc`ZJa]`]Uf]gY`ghi XYbhg`k]h\`\_Ym]ggi Yg`UbX`WcbWYdhg`]b`h\Y`Wci fgY

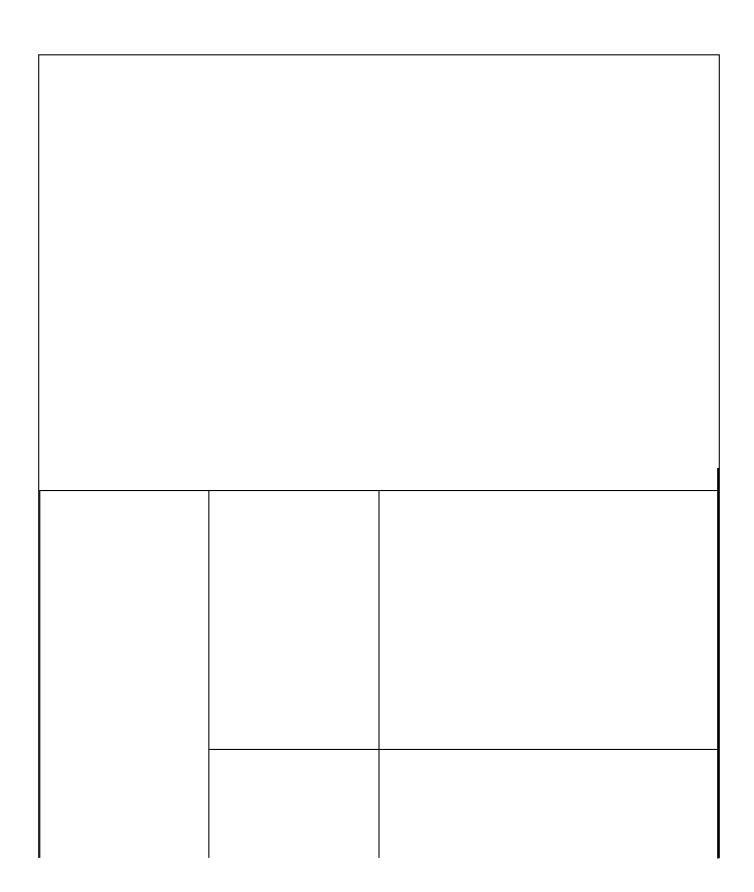
Œ```[fcidX]qWqq]cb'cZ]qqiYq'fU]qYX'Vm`YWifYq'UbX'aUhYf]U``]b'WcifqY'fYUXYf

Œ```WcgY`fYUX]b[`UbX`hYI h'U``UbU`mg]g`cZgYhhYI hg`hc`XYj Y`cd`Wf]h]WU``g\_]``g

Œ```c\\\Ugg`[fcid'YIYf\\]gYg

E····ha Y·U``cWJhYX·ZcfYUVX·gh XYbhihc·cZZYf'h\Y]f'ck b·cd]b]cb

Œ```bc`gYhei Ygh]cbg`Zcf`a U'cf`YggUmhc`YbWci fU[Y`ghi XYbhg`hc`fYgYUfW\'h\Y`hcd]Wg`k\]W\`a cgh`]bhYfYgh h\Ya ž'UbX`hc`dfcj ]XY`h\Ya `k ]h\`h\Y`cddcfhi b]hmhc`a U\_Y`h\Y]f`ck b`cf][]bU``]bhYfj Ybh]cb`]b`U`gW\c`Uf`m XYVUhY



		@cff]Y`AccfYfgi`" <ck'hc'hu`_'hc'mcif'ach\yf fBchYgŁ"</ck'hc'hu`_'hc'mcif'ach\yf 
K YY_'(.'%%'A UfVX'!'%+ A UfVX	@YWh fY	Mci 'Hu`_]b[ 'hc'a Y3. 'Z]bX]b[ 'h\Y'HfUWY'cZh\Y'bUffUhcf
		·
		dWSV[Ye
		>Ua YgʻD\Y`Ubžʻ±otfcXi Whjcbʻtcʻ7j bWdW U[Y 8[Uf[a`, <gvyw_w bobydwe[a`et="" fet="" fzwdzwfad[us^<br="" s`v="">FZWaok aX@SobSf[hW</gvyw_w>
		GigUb`@UbgYfz`"HckUfXg``U`:Ya]b]ghDcYh]Wg`cZ BUffUh]jY`Jc]WY"`Zfca`8[Uf[a`eaX3gfZad[fk,Ia_W Id[fWdeS`V@SddSf[hWHa[UW
		F]W.\UfX`K U`g\ž"H\Y`BUffUhcf`UbX`h\Y`: fUa Y`cZ :]Whjcb"`Zica `FZWDZWfad[UaX8[Uf[a`S/fk,@SddSf[hW FZWadkS`VfZW;VWSaX8[Uf[a`
		F]WkUfX`5WhY`ž" <yuf]b[`jc]wkg`]b`buffuh]jy`hyi hg"`<="" td=""></yuf]b[`jc]wkg`]b`buffuh]jy`hyi>
	GYa ]bUf	: cWU`]nUh]cb
		G\cfnZJWNjcb.
		>i`]Ub`7cffUnUUffig`"H\Y`7cbh]bi]micZDUf_g"
		F]W_'AccXmfg'"H\Y'; f]X"
K YY_`).`% `A UfVX`!`&( A UfVX	@YWh fY	≠ig'U'a UmiYf'cZhfi gh'i bfY`]UV`Y'bUffUhjcb'UbX'h\Y ]a d`]YX'Ui h\cf
		dMSV[Ye
		; fYtU'C`gcbž"FYWcbg]XYf]b['I bfY`]UV]`]tm': U``]V`Y UbX'I btfi gtk cft\mBUffUtcfg"
		5bg[Uf'Bibb]b[ž"FYWcbWYdhiU`]n]b['IbfY`]UV`Y BUffUh]cb. 'Gmbh\Yg]n]b['7c[b]h]jY'UbX'F\Yhcf]WU` 5ddfcUW\Yg"
		6fi bc'NYfk YW_ž"<]ghcf]Wjn]b['I bfY`]UV`Y'BUffUhjcb. I bfY`]UV]`]hmUbX'7 i `hi fU`'8]gWci fgY']b'BUffUhjj Y :]Wfjcb"
		6f]Ub F]W.UfXgcbž"ad`]YX 5ih.cfgž<]ghcf]WU` 5ih.cfgžUbX h.Y HfUbgdUfYbhBUffUhcf. Hck UfXg U BYk AcXY`cZh.Y BUffUh]jY HfUbgUWJcb" Zca

1		G``SfgdS^Ha[UWe
	GYa ]bUf	<u> </u>

	GYa ]bUf	>a '[fS
K YY_"%\$."&&"5df]`"!"&, 5df]`	@YWn fY	A W9k Ub'g'3fa`W_Wf.'Cab]gW]Ybhz'AYhUZ]WNjcbU`UbX'IbfY`]UV`Y3
		dNSV[Ye
		>Ua YgʻD\Y`Ubžʻ"8Y`UmYX`8]gWcgi fYʻUbXʻh\Y DfcV`Ya `cZCh\Yf`A]bXg.`±Jb`AW9kUb'gʻ3fa` W_W f' Zfca `7j bWdW U[`Y8[Uf[a`
		6f]Ub`: ]bbYmž"6f]cbmg`GHUbX`5[U]bghCV`]j ]cb.`H\Y AU_]b[`cZ: ]Wf]cb`]b`+Ub`A W9k Ub'g`3fa` W_ W f
	GYa ]bUf	3 fa`W_W f
K_YY_''‱'&- '5df]`'!'% A_Um	@YWhifY	: ]WMjcbU`]hm`BY]h\Yf`Hfi h\`bcf`@]Yg
		DWSV[Ye
		>c\b'GYUfYž"H\Y'@c[]WU`GHUH g'cZ:]WNjcbU` 8]gWcifgY"'f%+)Ł'
		8 cff]h7 c\bž"G][ bdcghg cZ: ]W]cbU`]hm 5 B UffUhc`c[ ]WU``DYfgdYW]j Y" f% Ł
		@ Vca Ér8cY Yž"FYdfYgYbHJHjcbcZH\YDUghUbX Dcgg]VYK cfXg"f&\$%\$Ł
		B]Y`gYbž'K U`g\ž'D\Y`Ubž'"HYb'H\YgYg'5Vci h : ]W¶cbU`]m"'f&\$%) Ł'
		DUi ``8Uk gcbž"HYb'H\YgYg'5[U]bgh:]WjcbU`]mi' f&\$%) Ł
	GYa ]bUf	3fa` W_ W f

# Fygci fWyg

# DfYgWf]VYX F Ygci fWYg

- J`UX]a ]f BUVc\_cj ž>a ⟨fS
- Jb A W9k Ubž 5ftac W\_ W f

 $H\Y @]j ]b[ < UbXVcc\_cZBUffU$ 

- °9 Xk UfX °D" °>cbYgž FZW=`ai` laďV

# FYWca a YbXYX FYgci fWYg

### FYWca a YbXYX fYUX]b[.

; YfUfX'; YbYffY'''@SddSf[hW6 [eUagdeW 3` 7 eeSk [` ? WfZaV'''% +&"''HfUbg"'>UbY'9"'@Yk ]bž' $\pm$ h\UWU. '7 cfbY`` I Dž'% , \$"

Cb`]bY'fYgci fWyg.

 $-\text{`}FZW>[h[`Y:S`VTaa]\ aX@SddSfa^aYk.`\ hd.#k kk"`\b"ib]! \UaVif["XY"]$ 

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

\_Zmci YbWci bhYf'U'dfcV`Ya 'k \Yb'UhYa dhJb[ 'hc'gi Va ]hmci f'Ugg][ ba Ybhh\fci [ \ 'Hi fb]hJbž'd`YUgY
hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-', ) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft'' =Zmci
UfY'i bUV`Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZUi 'hk ]h\'Hi fb]hJb'mci 'a Um'Udd'mZcf'Ub'Y! hYbg]cbžVi hmci
a i ghfYhU]b'mci f'hJW\_Yhbi a VYf'Zfca '9! hYfbU``Gi ddcfhfU'cb[ 'k ]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj ]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'' =Zmci 'Ya U]`'9! hYfbU``Gi ddcfhmci 'k ]``

### 5 WUXYa | W < cbYghmUbX D`U[ | Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU\_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b[ 'WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW\_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf\_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k\YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b[ 'U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b[ 'h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k ]h\ci hUW\_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k ]h\ci hWfYX]hUbX'hc d]YW]b[ 'hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b[ "

7 c``i g]cb. 'k cf\_]b[ 'k ]th 'cth Yfg'Vi hidUgg]b[ 'cZZth Y 'k cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7 c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b[ 'mci f'k cf\_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfglUbX`mci f`f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'Uhi BGK
- VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hzil BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5WWdhUV`Y'I gY'cZ I BGK '= H'F Ygci fWfg'Dc`]Wh
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWhYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wcaaib]hm
- `cWUHY 'gYfj ]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

### 5 WUXYa ]W = b Zcfa Uh cb ·

: cf`YggYbhJU``gh XYbh`]bZcfa UhJcb`fY`UhJb[ 'hc.

- fYei Yghg Zcf Yl hYbg]cb/
- `UhY`gi Va ]gg]cbg`[i ]XY`]bYg/
- fYj ]Yk 'cZa Uf\_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]W[Yg/
- YI Ua ]bUhcb dfcWXi fYg/
- gdYWJU``Wcbg]XYfUHjcb`]b`H\Y`Yj YbhcZ]``bYgg`cf`a ]gUXj Ybhi fY/
- gh XYbhYei ]lmUbX X]gUV]`]lm/
- UbX'ch\Yf'YggYbhJU`'UWUXYa ]W]bZcfa UhJcbž'gYY

\hdg.#k k k "Uffg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa ]W]bZcfa Uf]cb#dfchcWc`g![i]XY`]bYg#

.

# a U[Y'7fYX]h

5 i gh|b \*&\$% 'G\]`]b[ 'K i

#### 7F = 7CG

7F = 7CG Dfcj ]XYf 7cXY. \$\$\$-,;