



# **ARTS3052**

HYfa 'C bY''##'&\$%-

### 7ci fgY'Cj Yfj ]Yk

#### Ghuzz 7 cbhuWh8 Yhu]`g

#### '7cbj Ybcfg'

BUa Y	9a U]`	5j U]`UV]`]m	@cWJhjcb	D\cbY
9a a Uʻ>UbY	Yaa U"^UbY4 i bgk "YXi "Ui	-	‰) ž@YjY``%ž FcVYfh KYVghYf	

#### GWkcc~7cbhJWh~abZcfa Uh]cb

Fcca " &ž`Yj Y`" FcVYfhK YVghYf`6i ]`X]b[

D\cbY.'f\$&E'-',)'(,)\*

9a U]` gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.#gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7i gtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[tcb'WJa di g\cong tz'; UX][U'`fP]tmUbX'5fth/ '8Yg][b'7Ua di gYg\cong tubX't\Y'B[i bbUk U` dYcd'Y'fbi gtfU']Ub'8YZYbW': cf\w'5\\WXYa m']b'7UbVYffU\cozh\Y'`UbXg'k\YfY'YUW\cozh\Y'YUW\cozh\Y''UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'''\UbXg'k\YfY'YUW\cozh\Y''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'$ 

#### 7ci fgY'8YW]`g

7 fYX]hDc]bhg\*\*

Gi a a UfmcZh\Y 7ci fgY

Gi VYWh5fYU. 7`Y/[eZ

H\]g`Wci fgY`dfcj ]XYg`mci `k ]h\`Ub`cddcfhi b]lmhc`i bXYffU\_Y`k cf\_!]bhY[ fUhYX``YUfb]b[ `UbX`[ U]b`]bXi ghfm YI dYf]YbW'`k ]h\`U`\cghcf[ Ub]gUh]cb`WcgY`mfY`UhYX`hc`mci f`A U`cf`]b`9b[`]g\"`Mci `a UmU`gc`Udd`mhc`k cf\_cb`UhtUWA Ybhcb`Ub`UWUXYa ]WfYgYUfW\`dfcYWhcf`k cf\_]b`Ub`YX]hcf]U``fc`Y`Zcf`Ub`UWUXYa ]Wfci fbU`" =XYU``mz`mci `k ]``i bXYfhU\_Y`Ub`]bhYfbg\]d`UZhYf`mci `\Uj Y`Wca d`YhYX`%") `mYUfg`cZZ``!h]a Y`ghi Xmfcf Yei ]j U`Ybhz'UbX`Wca d`YhYX`U`a ]b]a i a `cZ% `I C 7 `]b`h\Y`A U`cf"`5hih\Y`YbX`cZh\Y`]bhYfbg\]d`mci `k ]`` dfcj ]XY`U`gi a a Uh]j Y`fYdcfhcZmci fYI dYf]YbWg`UbX`k cf\_YI Ua d`Yg`Wca d`YhYX`Xi f]b[ `h\Y`]bhYfbg\]d"

H\Y']bhYfbg\]d'fYei ]fYg'U'rchU``Wca a ]ha YbhcZ%\$\$!%) \$`\ci fg'cZk cf\_'k ]h\'U'\cghcf[ Ub]gUh]cb'UbX'a Um bcfa U``m'VY'hU\_Yb']b'Z]fghžgYWcbX'cf'gi a a Yf'gYa YghYf'' =bhYfbg\]d'cddcfhi b]h]Yg'UfY'UXj Yfh]gYX'j ]U'h\Y GW\cc``cZh\Y'5fhg'UbX'A YX]U' =bhYfbg\]d'BYk g'YhYf''5'hYfbUh]j Y`mmci 'a UmUddfcUW\'U'fY'Yj Ubh cf[ Ub]gUh]cb'hc'Udd`mZcf'Ub']bhYfbg\]d'''Df]cf'hc'gYY\_]b[ 'Ub']bhYfbg\]dz'mci 'g\ci `X'UhYbX'Ub']bhYfbg\]d ]bZcfa Uh]cb'gYgg]cb'fi b'Vmh\Y'GW\cc``cZh\Y'5fhg'UbX'A YX]U''

Hc VY Y`][ ]V`Y Zcf'h\]g Wci fgYzmci a i gh\Uj Y U a ]b]a i a 'K 5A 'cZ+\$"

#### 7 ci fgY @YUfb]b[ 'Ci hWca Yg

%" \Uj Y`[ U]bYX`YI dYf]YbW`cZ]bXi ghfmdfc\WggYg`UbX`dfU\Wj\Wg &" Udd`mh\YcfYhj\Wb``Wcb\Wdhg`UbX`dfU\Wj\\Wb``g\_]``g`[ U]bYX`]b`h\Y`dfc[ fUa `hc`fYU`!k cfX`\\chi\Y hg \\ ' " \Uj Y`Yb\Ub\\X'h\Y]f`\\Ud\\Jhm\Zcf`]bXYdYbXYbhYb[ U[ Ya Ybhk ]h\`]bXi ghfmdfcj ]XYfg

#### HYUW ]b[ 'GhfUhY[ ]Yg'

 $H\ ]g'Wci\ fgY'\ Ug'bc'Zcfa\ U`'hYUW\]b[\ 'Wca\ dcbYbh'''$ 

# 5ggYgga Ybh

### 5ggYgga Ybh'HUg\_g

5ggYgga Ybh'hUg_	K Y][\h	8iY'8UhY	Gh XYbh@YUfb]b[ Ci hWca Ygʻ5ggYggYX
7 f]hJWU`F YZYWJcb'	) \$1		

- 7 ca d`Yhjcb`cZU`a ]b]a i a `cZ%\$\$`\ci fg`cZd`UW\a Ybh
  Gi Va jagojk\bogdbijtUgogh\goga YbtahUg\_g`%\bog\X\ra cbghfusto[`U`gYf]ci g`Uhn\a dh\nec`ijtNgk\rbh\y`hUg\_fYei ]fYa Ybhg

i]fYaYb

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

\_Zmci YbWci bhYf'U'dfcV`Ya 'k \Yb'UhYa dhJb[ 'hc'gi Va ]hmci f'Ugg][ ba Ybhh\fci [ \ 'Hi fb]hJbž'd`YUgY
hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-', ) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft'' =Zmci
UfY'i bUV`Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZUi 'hk ]h\'Hi fb]hJb'mci 'a Um'Udd'mZcf'Ub'Y! hYbg]cbžVi hmci
a i ghfYhU]b'mci f'hJW\_Yhbi a VYf'Zfca '9! hYfbU`'Gi ddcfhfU'cb[ 'k ]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj ]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'''=Zmci 'Ya U]`'9! hYfbU`'Gi ddcfhmci 'k ]``

#### 5 WUXYa | W < cbYghmUbX D`U[ | Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU\_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hUW\_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b[ 'WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW\_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf\_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k\YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b[ 'U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b[ 'h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k ]h\ci hUW\_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k ]h\ci hWfYX]hUbX'hc d]YW]b[ 'hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b[ "

7 c``i g]cb. 'k cf\_]b[ 'k ]th 'cth Yfg'Vi hidUgg]b[ 'cZZth Y 'k cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7 c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b[ 'mci f'k cf\_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi V'YWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY