



ARTS3095

65 A YX]U + hYfbg\]d

HYfa 'C bY''##'&\$%-

7ci fgY'Cj Yfj]Yk

Ghuzz 7 cbhuWh8 Yhu]`g

'7cbj Ybcfg'

BUa Y	9a U]`	5j U]`UV]`]m	@cWJhjcb	D\cbY
9a a Uʻ>UbY	Yaa U"^UbY4 i bgk "YXi "Ui	-	‰) ž@YjY``%ž FcVYfh KYVghYf	

GWkcc~7cbhJWh~abZcfa Uh]cb

Fcca " &ž`Yj Y`" FcVYfhK YVghYf`6i]`X]b[

D\cbY.'f\$&E'-',)'(,)*

9a U]` gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.#gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7i gtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[tcb'WJa di g\cong tz'; UX][U'`fP]tmUbX'5fth/ '8Yg][b'7Ua di gYg\cong tubX't\Y'B[i bbUk U` dYcd'Y'fbi gtfU']Ub'8YZYbW': cf\w'5\\WXYa m']b'7UbVYffU\cozh\Y'`UbXg'k\YfY'YUW\cozh\Y'YUW\cozh\Y''UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'''\UbXg'k\YfY'YUW\cozh\Y''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'$

7ci fgY 8YHJ] g

7 fYX]hDc]bhg *

Gi a a UfmcZh\Y 7ci fgY

Gi VYWn5fYU. ? WW[Sł 5g/fgdWS` V FWUZ` a 'aYk

H\]g`Wci fgY`dfcj]XYg`mci `k]h\`Ub`cddcfh b]hmhc`i bXYffU_Y`k cf_!]bhY[fUhYX`YUfb]b[`UbX`[U]b`]bXi ghfm YI dYf]YbW'k]h\`U`\cghcf[Ub]gUh]cb`WcgY`mfY`UhYX`hc`mci f`A U`cf`]b`A YX]Už`7 i `hi fY`UbX`HYW\bc`c[m'i Mci a UmU`gc`Udd`mhc`k cf_`cb`UhtuW\a Ybhicb`Ub`UWUXYa]WfYgYUfW\`dfc`YWficf`k cf_`]b`Ub`YX]hcf]U``fc`Y`Zcf`Ub UWUXYa]W`ci fbU`"'=\XYU``mž`mci `k]```i bXYfhU_Y`Ub`]bhYfbg\]d`UZhYf`mci `\Uj Y`Wca d`YhYX`%") `mYUfg`cZZ\``!h]a Y ghi Xmfcf`Yei]j U`Ybhz`UbX`Wca d`YhYX`U`a]b]a i a `cZ% `I C 7 `]b`h\Y`A U`cf"'5hh\Y`YbX`cZh\Y`]bhYfbg\]d`mci k]```dfcj]XY`Uʻgi a a Uhj Y`fYdcfhcZmci f`YI dYf]YbWfg`UbX`k cf_`YI Ua d`Yg`Wca d`YhYX`Xi f]b['h\Y`]bhYfbg\]d"

H\Y']bhYfbg\]d'fYei]fYg'U'rchU``Wca a]ha YbhcZ%\$\$!%) \$`\ci fg'cZk cf_'k]h\'U'\cghcf[Ub]gUh]cb'UbX'a Um bcfa U``m'VY'hU_Yb']b'Z]fghžgYWcbX'cf'gi a a Yf'gYa YghYf'' =bhYfbg\]d'cddcfhi b]h]Yg'UfY'UXj Yfh]gYX'j]U'h\Y GW\cc``cZh\Y'5fhg'UbX'A YX]U' =bhYfbg\]d'BYk g'YhYf''5'hYfbUh]j Y`mmci 'a UmUddfcUW\'U'fY'Yj Ubh cf[Ub]gUh]cb'hc'Udd`mZcf'Ub']bhYfbg\]d'''Df]cf'hc'gYY_]b['Ub']bhYfbg\]dz'mci 'g\ci `X'UhYbX'Ub']bhYfbg\]d]bZcfa Uh]cb'gYgg]cb'fi b'Vmh\Y'GW\cc``cZh\Y'5fhg'UbX'A YX]U''

Hc VY Y`][]V`Y Zcf'h\]g Wci fgYzmci a i gh\Uj Y U a]b]a i a 'K 5A 'cZ+\$"

7 ci fgY @YUfb]b['Ci hWca Yg

%" \Uj Y`[U]bYX`YI dYf]YbW'cZ]bXi ghfmdfcWfggYg`UbX`dfUWf]\Wg &" Udd`mh\YcfYh]\Wb``WcbWfdhg`UbX`dfUWf]\Wb``g_]``g`[U]bYX`]b`h\Y`dfc[fUa `hc`fYU`!k cfX`WcbhYI hg \" \Uj Y`Yb\Ub\WfX`h\Y]f`\Wdd\W]\mZcf`]bXYdYbXYbhYb[U[Ya Ybhk]h\`]bXi ghfmdfcj]XYfg

HYUWX]b['GhfUhY[]Yg'

 $H\]g'WcifgY'\Ug'bc'ZcfaU'hYUWX]b['WcadcbYbh'''$

5ggYgga Ybh

H\]gʻgi VYWhjgʻi b[fUXYXʻgcʻUʻdUggʻ]gʻXYdYbXYbhcbʻGUhjgZJWhcfmifGMŁcfʻI bgUhjgZJWhcfmifI @Ł`]bʻa YYhjb[h\Y`Wci fgY`fYei]fYa Ybhg"ʻ5bʻGM[fUXY`k]``bchUZYWhmci f`kY][\hYX`Uj YfU[Y`a Uf_`fK 5A Ł'Vi h'U': @'[fUXY k]``''

7 ci fgY fYei]fYa Ybhg]bWl XY.

- 7 ca d'Yhjcb'cZU'a]b]a i a 'cZ%\$\$'\ci fg'cZd'UWa Ybh
- Gi Va]gg]cbg`cZUggYgga YbhitUg_g`%/`&`XYa cbghfUh]b[`U`gYf]ci g`UhhYa dhitc`Ubgk Yf`th\Y`tUg_fYei]fYa Ybhg

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

 $H\YfY\UfY\bc\dfYgWf]VYX\fYgci\fWYg\Zcf\h\]g\Wci\fgY"$

FYWca a YbXYX FYgci fWYg

7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

@f]YZmci h]bY`\ck 'ghi XYbhZYYXVUW_flVch\ 'Zcfa U``UbX`]bZcfa U`E'cb'h\Y`Wci fgY`k]``VY`[Uh\YfYXž\ck ']h k]``VY`UbU`mgYX`UbX`\ck ']hk]``VY`UbU`mgYX`UbX`\ck ']hk]``VY`UbWYX`i dcb'hc']a dfcj Y`h\Y`ghi XYbh`YUfb]b['YI dYf]YbWY'': cf'YI Ua d`Yž mci 'a][\hX]gW gg`k \Uhk Ug`]XYbh]Z]YX`]b'dUghZYYXVUW_UbX`\ck 'h\]g'Wci fgY`k Ug'W\Ub[YX`hc'UXXfYgg`h\Y]ggi Y"Q

Gi Va |gg|cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwci bhYf'U'dfcV'Ya k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybht\fci [\ 'Hi fb]hJbž'd'YUgY

HY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-',) '' ' ' %cf'Ya U] 'h\Ya 'cb'Y! hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'\\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUfŁ" Image:

UfY'i bUV'Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]hJb'mci 'a UmUdd'mZcf'Ub'Y! hYbg]cbž'Vi hmci
a i ghfYhJ]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hYbg]cb'Udd']WUh]cb" Image: Ya U]''9! hYfbU''Gi ddcfhmci 'k]''

Ui hca UhJWJ''mfYW'] Y'U'hJW_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]'''bYYX'hc'gdYWJZWJ''mUg_'Zcf'cbY"

Hi fb]hJb'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf"

; YbYfU``mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\W)``mj]U'Y]h\Yf'Hi fb]hjb'cf'U'A ccX`Y Ugg][ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]``'VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\ U`hYfbUhj Y'gi Va]gg]cb'XYHJ]`g''

cfi]bZcfa Uh]cbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbh'i bgk "YXi "Ui #\ck! qi Va]hUgq][ba Ybha ccXiY

5 WUXYa | W < cbYghmUbX D`U[| Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_]b['k]th 'cth Yfg'Vi hidUgg]b['cZZth Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY