

# 7ci fgY<sup>-</sup>Cj Yfj ]Yk

## GHJZ7cbHJWh8YHJ]`g

#### 7cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
A cb]WU-6cUfXa Ub	a "VcUfXa Ub4 i bgk "YXi "Ui	6m5ddc]bha Ybh		

### GWXcc`7cbHJWh =bZcfa Uh]cb

GWkcc~cZ9Xi WUhcb

 $5 fhg \ddot{z} 8 \Upsilon g][b Ub X 5 fW ]h W f f Y$ 

; fci bX': `ccfž'A cfj Yb'6fck b'6i ]`X]b[ 'fl &\$Ł

H. 'Ž \* %'f&Ł'-',) '%-++

9. YXi WUhjcb4 i bgk "YXi "Ui

K.\hdg.#kkk"Ufhg"i bgk "YXi "Ui #YXi WUhjcb

#### 5W\_bck `YX[ Ya YbhcZ7ci bhfm

 $\label{eq:localized-loca$ 

 $\label{eq:continuous} \text{$\overset{\cdot\cdot}{=}$ U[Y'WciftY'gmcZhY'CZhY'Dfc'J]WY!7\twww.$``cf'$$ bX][Ybcig']$ $$BGK_{$^{\circ}}$$ bX][Ybcig'ghfUhY[m]$$ $$$ 

## 7ci fgY 8YHJ] g

#### $I b hg c Z 7 f Y X h^*$

#### K cf\_`cUX

%) \$`\ci fg`]bWi X]b[`WUgg`WcbHUWh\ci fgž`fYUX]b[gž`WUgg`dfYdUfUh]cbž'UggYgga Ybhž'Zc``ck 'i d`UWh]j]h]Ygž YhW

#### Giaa UfmcZh\Y 7ci fgY

 $YZd Zd R Yj ScZU T`fcdV \ddot{z}; eZd RgR2RS]V e`S`eY f_UVcXcRUfReV R_U a`deXcRUfReV def UV_ed \ddot{z} YV T`fcdV T`_eV_e UV]ZgVg R_U RddVdd^ V_eh2]SV ZUV_eZR] WcS`eY Xc`fad`Wdef UV_ed \ddot{z} YV T`fcdV T`_eV_e UV]ZgVg R_U RddVdd^ V_eh2]SV ZUV_eZR] WcS`eY Xc`fad`Wdef UV_ed \ddot{z} YV T`fcdV T`_eV_e UV]ZgVg R_U RddVdd^ V_eh2]SV ZUV_eZR] WcS`eY Xc`fad`Wdef UV_ed \ddot{z} YV T`fcdV T'fcdV T'fcdV$ 

±0.1h.]g.Wei fgYžmci ik]```YUfb`\ck ihc'hYUW.'J]gi U``5fhg'Uh'Ub'UXj UbWYX``Yj Y``]b'gYWebXUfmWebhYI hg"'Mei k]``i gY'fY`Yj Ubhgm`UVi g'XeW a Ybhg'hc'XYj Y`ed']bbcj Uhjj Y'UbX'Yb[ U[ ]b[ ``Yggcb'd`Ubg'UbX'W ff]W`i a d`Ubg"'Mei ik]```YUfb'UbX'dfUWjgY'U'fUb[ Y'eZhYUW.]b[ 'ghfUhY[ ]Yg'h\Uha Ul ]a ]gY'h\Y``YUfb]b[ 'dehYbhJU``eZ U``'hmdYg'eZ`YUfbYfg']b'U'gUZYžgi ddefhjj Yž'UbX'\][ \`mYb[ U[ YX'WUggfeea 'Ybj ]feba Ybh''Mei 'k]``XYg][ b Zef'UbX']a d`Ya Ybh'hYUW.]b[ 'ghfUhY[ ]Yg'h\Uh]bWefdefUhY'X][ ]hU``UbX'eh\Yf]bbcj Uhjj Y'ghfUhY[ ]Yg''Mei 'k]``U'ge``YUfb'UVei hU'fUb[ Y'eZUggYgga Ybh'UbX'ZYYXVUW\_'ghfUhY[ ]Yg']b'h\Y'X]gWJd`]bYžk ]h\`U'ZeW g'eb UggYgga Ybh']b'h\Y'gYb]ef'gYWebXUfmgWkee`"

#### 7 ci fgY @YUfb]b[ Ci hWca Yg

- %" ⇒ YbhjZmYggYbhjU``Y`Ya Ybhg`cZh\Y`B9G5`J]gi U``5fhg`Gm``UVi gžUbX`ghfUhY[]Yg`hc`gi ddcfhighi XYbhg Ug`h\YmihfUbq]hjcb`VYkk YYb`ghU[Yq
- &" I gY`glfcb[ `\_bck `YX[ Y`cZgi V^YWiWcbhYbhhc`d`Ub`UbX`Yj U`i UhY`Wc\YfYbhž`[ cU`!cf]YbhYX`UbX WXU``Yb[ ]b[ ``Yggcbgž``Yggcb`gYei YbW'g`UbX`hYUWX]b[ 'dfc[ fUa g`k \]W\ k ]```Yb[ U[ Y`U```ghi XYbhg
- ' "GYhUWX]Yj UV`Y``YUfb]b[ 'ci hWca Y#]bhYbh]cbg'hc'a UhWX`WcbhYbhž'hYUWX]b[ 'ghfUhY[ ]Ygž'fYgci fWYg'UbX X]ZZYfYbh'hmdYg'cZUqqYqqa Ybh'Zcf'U'i b]hcZk cf\_`]b'J ]qi U``5fhq
- ("Dfcj]XY'WYUf'X]fYWIcbg'hc'cf[Ub]qY'UbX'qiddcfhdfYdUfYX'UWIj]hIYq'UbX'iqY'fYqcifWYq
- ) " 5ggYgg UbX fYdcfhcb gh XYbh YUfb]b[ ']b J ]gi U` 5fhg hc U`` \_YmghU\_Y\c XYfg
- \*"=XYbhjZmh\Y`W\UfUWhYf]ghjWg`cZUb`YZZYWhjjY`J]giU``5fhg`hYUW\Yf`UbX`h\Y`ghUbXUfXg`cZdfcZYgg]cbU`dfUWhjWY`]b`hYUW\]b[zYgdYWjU``mh\Y`Uhhf]VihYg`cZ; fUXiUhY`hYUW\Yfg

#### 5 i glfU`]Ub DfcZYgg]cbU`GlUbXUfXg Zcf HYUWX Yfg

GHUbXUfX	•	5ggYgga Ybh#g
%"%"%	8Ya cbglfUlY'_bck `YX[Y'UbX'i bXYfglUbX]b['cZd\mg] <b>\u00fab</b> 'ž	ł
	gcWJU`žUbX`]bhY``YWhU`XYjY`cdaYbhUbX`WXUfUWhYf]ghJWg`cZ	
	ghiXYbhgʻUbX`\ck`h\YgY`aUmUZZYWh`YUfb]b[	
%"&"%	8Ya cbglfUllY'_bck  YX[ Y'UbX'i bXYfglUbX]b[ 'cZfYgYUfW\']blc	ł
	\ck 'gh XYbhg``YUfb`UbX`h\Y`]a d`]WUh]cbg`Zcf`hYUVX]b[	
%"' "%	8Ya cbghfUhY`_bck`YX[Y`cZhYUWX]b[`ghfUhY[]Yg`h\Uh'UfY	%ž <sup>*</sup> &
	fYgdcbg]j Y'lo'lh\Y'`YUfb]b['glfYb[h\g'UbX'bYYXg'cZghi XYbhg	
	Zfca X]j YfgY`]b[i]gh]WgžW`hifU`žfY`][]cigžUbX	
	gcWcYWcbca ]WVUW_[fci bXg	

# 5ggYgga Ybh

5ggYgga Ybh'tUg_	K Y][ \h	8iY'8UHY	7 ci fgY @YUfb]b[ Ci hWca Yg 5ggYggYX
%"'GWcdY'UbX'gYei YbW	(\$1	\$&#\$, #&\$&&`\$).\$\$`DA</td><td>&ž' ž'( ž')</td></tr><tr><td>&"'I b]hcZkcf_</td><td>* \$1</td><td>&' #\$, #&\$&&`\$).\$\$`DA</td><td>%ž' ž'( ž'*</td></tr></tbody></table>	

#### 5ggYgga Ybh% GWcdY UbX gYei YbWY

8i Y'XUhY. \$&#\$, #&\$&&\*\$).\$\$DA

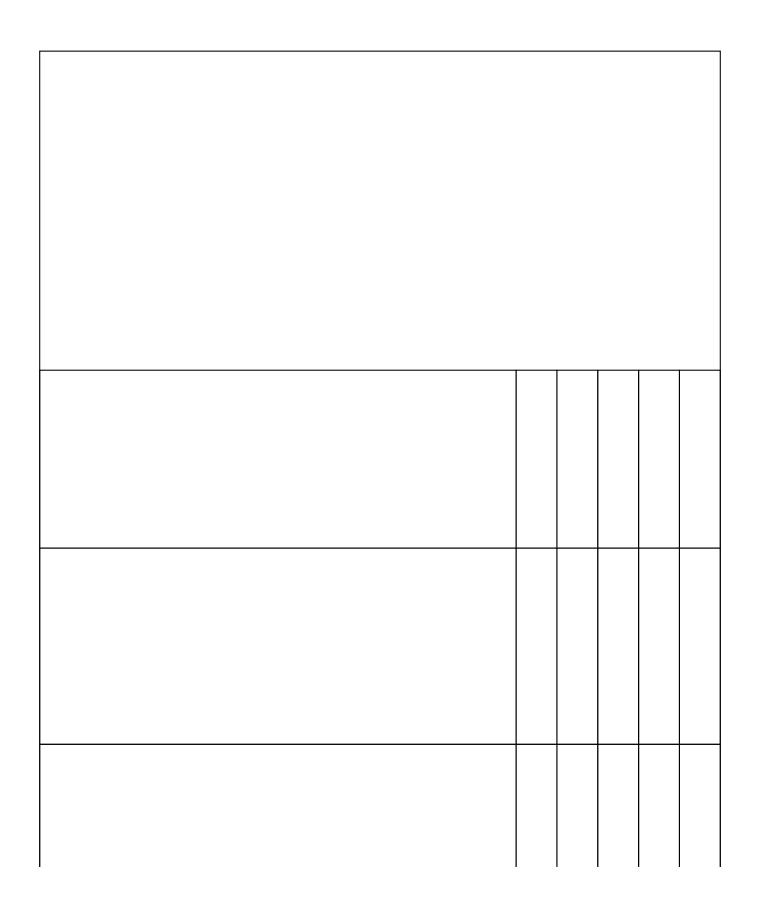
7 fYUHY 'U'gWcdY 'UbX'gYei YbWYž]bWi X]b[ 'YUfb]b[ 'ci HWca Ygž'Wcj Yf]b[ '%\$'k YY\_g'Zcf'U'MYUf' '%'dfY`]a ]bUfm WUgg"'DfYdUfY 'Ub'UggYgga Ybh'HUg\_'h\Uh'X]fYWhm`]b\_g'hc'h\Y'HYUW\]b[ 'UbX''YUfb]b[ ']bHYbh]cbg'Zcf'h\Y HYfa 'g'k cf\_"'=\xi\X]WUhjj Y''Yb[ h\.`&\\$\\$k cfXg"

5 ZYYXVUW\_g\YYhk]``'VY'dfcj]XYX"

#### 5XX]h]cbU`XYhJ]`g

D5FH'% '7 fYUhY 'U'gWcdY 'UbX'gYei YbW'ž']bWi X]b[ 'YUfb]b[ 'ci hWca Ygž'Zcf'U'hM'Uf'\%fDfY`]a ]bUfmŁ'J ]gi U`5fhg'Wci fgY"'

D5FH-&: 7\ccg]b[ 'Zfca 'CB9'i b]hZfca 'mci f'GWcdY'UbX'GYei YbWfz'dfYdUfY'U'Wca V]bYX'UggYgga Ybh



¨flŁ—			 2fŽŁ
	···flt-	"fl\	"fle

GdYW]ZJW7f]hYf]U	··flŁ—		 2fŽŁ
Ghfi Whi fY'UbX'cf[Ub]gUh]cb'cZfYgdcbgY			
8Ya cbglfUhYgʻUV]`]lmihcʻd`Ubʻi g]b[ 'VUW_k UfX'a Udd]b[ 'hc'a YYh gY`YWNYX'ci HWca Yg			
DfYgYbhUh]cb^cZYZZYWh]j Y^UbX^Yb[U[]b[^YUfb]b[^gYei YbWY			
• 9a VYXgʻfY`Yj UbhiUffk cfX'Yl Ua d`Yg			
DfYgYbhJhjcbicZifYgdcbgYiUWWcfX]b[ihciUddfcdf]UhYiUWUXYa]WUbXi]b[i]ghjWWcbjYbhjcbg			
• K f]hYg'i g]b[ 'W&ffYWh'GhUbXUfX'5i ghfU`]Ub'9b[`]g\			

# FYgci fWfg

### DfYgWf]VYX F Ygci fWYg

#### FYei ]fYX fYUX]b[g

 $\label{thm:linear} $$ Mci 'UfY'fYei ]fYXZ'Zcf'h\]g'Wci fgYZ'UbX']b'h\Y'Z hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\][\mbox{$\mathbb{n}$ inclined } fgY'Z' hi fYZ'hc'\Uj Y'Wcd]Yg'cZh\Y'gm`UVi g'XcW a Ybhg''' + i]g'\Y'Ui g'XcW a Ybhg''' + i]g'\Y'Ui g'XcW a Ybhg''' + i]g'\Y'Ui g'XcW a Ybhg''' + i[g'X'Y'' hi fYZ'' hi fYZ''' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ''' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ''' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'' hi fYZ'''$ 

• 5i ghfu`]ub`7i ff]W`i a ž5ggYgga Ybhž'ubX`F Ydcfh]b[ '5i h\cf]hmfb75F5\!''f&\$\$-\!'' YRaV` WeYV 3fdexR]R\_5fczTf]f^, YV 3ced"'GmXbYmž'BGK ž5i ghfu`]u.'575F5"

# Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

# Hi fb]h]b Gi Va ]gg]cb

☐ Inc i YbWci bhYf U'dfc V`Ya ik \Yb 'UrhYa dh]b[ 'hc 'gi Va ]hmci f 'Ugg][ ba Ybhth\fci [ \ 'Hi fb]h]bž'd`YUgY

HY 'Yd\cbY'9I hYfbU``Gi ddcfhcb'-',) '' ' ' %cf 'Ya U] 'th\Ya 'cb'YI hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui ""'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ"' ☐ mci
UfY'i bUV'Y'hc 'gi Va ]hmci f 'Ugg][ ba YbhXi Y'hc 'U'ZUi 'hk ]h. 'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'YI hYbg]cbž'Vi hmci

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWbihU\_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUiqci fWYk]h\ci hUW bck iYX[Ya Ybh'

IBGK [fcidgdu[]Uf]ga ]bhch\YZc``ck]b[WUhY[cf]Yg.

7 cdm]b[. `I g]b[ 'h\Y'gUa Y'cf'j Yfmg]a ]`Uf'k cfXg'hc'h\Y'cf][ ]bU`'hYl hcf']XYU'k ]h\ci hUW\_bck `YX[ ]b[ 'h\Y gci fW'cf'i g]b[ 'ei chUh]cb'a Uf\_g"'H\]g']bWi XYg'Wcdm]b[ 'a UhYf]U`gž']XYUg'cf'WcbW'dhg'Zfca 'U'Vcc\_ž'Ufh]WYž fYdcfhcf'ch\Yf'k f]hhYb XcW a Ybhz'dfYgYbhUh]cbž'Wca dcg]h]cbž'Uffk cf\_ž'XYg][ bž'XfUk ]b[ ž'WfW ]hfmž'Wca di hYf dfc[ fUa 'cf'gcZk UfYž'k YVg]hYž']bhYfbYhz'ch\Yf'Y`YWfcb]WfYgci fW'z'cf'Ubch\Yf'dYfgcbfg'Ugg][ ba Ybhk ]h\ci h Uddfcdf]UhY'UW\_bck `YX[ Ya Ybh''

**Duddfcdf]UhY dufud\fug]b**[...7\ub[]b[...12\k...k.cfXg.UbX.d\fugYg.k.\]Y a cghmfYhJ]b]b[...h\Y.cf][]bU`]bZcfa Uh]cbžghfi Wh fY UbX#cfdfc[fYgg]cb.cZ]XYUg.cZh\Y.cf][]bU`k]h\ci hUW\_bck `YX[Ya Ybh'.H\]g.U`gc Udd`]Yg.]b`dfYgYbhUh]cbg`k \YfY gca YcbY dufUd\fugYg.Ubch\Yf'g.]XYUg.cf`k cfXg`k]h\ci h`WfYX]h`UbX`hc d]YW]b[...hc[Yh\Yf'ei chYg.UbX.dUfUd\fugYg.]bhc.U`bYk `k\c`Yžk]h\ci h`Uddfcdf]UhY`fYZYfYbW]b[...hc]

7c``i g]cb. K cf\_]b[ k ]h ch\Yfg'Vi hdUgg]b[ cZh\Yk cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b[ 'mci f'k cf\_'hc'Ubch\Yf'ghi XYbhZcf'h\Y'di fdcgY'cZh\Ya 'd`U[ ]Uf]g]b[ ždUm]b[ 'Ubch\Yf'dYfgcb'hc'dYfZcfa 'Ub'UWUXYa ]Whuq\_ž'ghYU`]b[ 'cf'UWei ]f]b[ 'Ubch\Yf'dYfgcb'g'UWUXYa ]Wk cf\_'UbX'Wcdm]b[

### 5 WUXYa ]W = b Zcfa Uh cb

: cf'YggYbhJU`gh XYbh]bZcfa UhJcb fY`UhJb[ hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
- `UhY`gi Va ]gg]cbg`[ i ]XY`]bYg/
- fYi ]Yk 'cZa Uf g/
- I BGK '< YU`h\ 'UbX'GUZYhmidc`]W[Yq/
- YI Ua ]bUhcb dfcWXi fYg/
- gdYWJU``Wcbg]XYfUhJcb']b'h\Y'Yj YbhcZ]``bYgg'cf'a ]gUXj Ybh fY/
- gh XYbhYei ]mrUbX X]gUV]`]m/
- UbX'ch\Yf'YggYbhJU''UWUXYa ]W]bZcfa UhJcbž'gYY

\hdg.#kkk"ibgk"YXi"Ui#Ufhg!XYg][b!UfW\]hYWhifY#ghiXYbhi`]ZY#fYgcifWYg!giddcfh#dfchcWc`g![i]XY`]bYg

#### a U[Y'7fYX]h

GmbYf[]Yg^]b^Gci bX^&\$%\*

#### 7F = 7CG

7 F = 7 C G 'Dfcj ]XYf'7 cXY. '\$\$\$-,;