

# **HUMS2000**

 $5 fhg^{+} \pm hY fbg \] d$ 

HYfa "Hk c" ## "&\$%

# 7 ci fgY Cj Yfj ]Yk

### 'GhUZZ'7cbhUWh'8YhU]`g'

### '7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWUh]cb	D\cbY
@ci]gY`GhXXm	O	6mUddc]bha Ybhj ]U Ya U]`	; )\$ <sup>*</sup> A cfj Yb 6fck b	-',)'%**%

### GWXcc`7cbHJWhi±bZcfa Uhjcb

GWXcc``cZGcWJU``GWJYbWYg

Fcca '%) -

A cfj Yb 6fck b 7 &\$

Ya U]`. 'gcgg4 i bgk "YXi "Ui

d\cbY. '\$&'-',) '% \$+

### 7ci fgY 8YW] g

7 fYX]hDc]bhg \* \*

#### Gi a a UfmcZh\Y 7ci fgY

Gi VYWh5fYU. 3dfe

 $H\ [g'Wci\ fgY'WUb'U'gc'VY'ghi\ X]YX']b'h\ Y'Zc``ck\ [b[\ 'gdYW]U']gUh]cbg.\ '5\ d\_[\ a'aYkl?\ WW[S/?\ WW[S/Ra`eS`V]Uf[a`fl?\ WW[S/EUdWW S`VEag`Vfl?\ WW[S/5a\_e` <agd Sfe_fl?\ WW[S/BgTf]UDWSf[a`eS`V 3VhWdf[e[`Yfi]UDWSf[a`eS`V 3VhWdf[e]`Yfi]UDWSf[a`eS`V 3VhWdf[e]$ 

H\Y`<I A G`&\$\$\$`Wci fgY`]g`Ub`Y`YWlj Y`]b`h\Y`I B GK `5flg`UbX`GcWJU``GWJYbWYg`dfc[fUa g`UbX`h\Y 7f]a]bc`c[ma U'cf`ghfYUa`]b`h\Y`6UW\Y`cf`cZDgmW\c`c[]\W\``G\WJYb\WYg`dfc[fUa "'=ha Um`VY`h\\_Yb`Uhh\Y`YbX cZU`ZfghmYUf`cZghi XmUbX`cZZYfg`ghi XYbhg`k cf\_'YI dYf]Yb\W`]b`U`fUb[Y`cZcf[Ub]gUh]cbg`i hj`]g]b[`gc\W]U`fYgYUf\W\`UbX`dc`]\midbX`\i a Ub]hYg`g\_]``g"

H\Y'j cWUMcbU``d`UWYa Ybhžk\]W\`]g`k cf\_YX`]b`h\Y`GmXbYma Yhfcdc`]hUb`UfYUždfcj ]XYg`k cf\_'YI dYf]YbWY UhU`\cghcf[ Ub]gUMcb`Zcf`%( 'Z ```XUmg`f%\$) `k cf\_]b[ `\ci fgŁ"'H\]g`dfUWJ\W\``YI dYf]YbWY`]g`UWWca dUb]YX`Vm U`fYUX]b[ `dfc[ fUa "'H\Y`fYUX]b[ `Wca dcbYbhYI Ua ]bYg`X]ZZYfYbhUddfcUW\Yg`hc`h\Y`gh XmcZcf[ Ub]gUMcbgž h\Y]f`ghfi Whi fYgž`Z bWJcbg`UbX`dc`]\JYgž'Ug`k Y```Ug``]b\_g`h\YgY`]ggi Yg`hc`h\Y`d`UWYa YbhYI dYf]YbWY"

BchY. "Ghi XYbhg'a i gh\Uj Y'UW\]Yj YX'U'WfYX]h``Yj Y``cf'VYhhYf'Uj YfU[ Y'UWfcgg'h\Y'Wci fgYg']b'h\Y]f`XY[ fYY" H\Y']bhYfbg\]d'a UmVY']bWi XYX'Ug'dUfhcZU'a U'cf'ghfYUa ']b'h\Y': UW'`hmdfc[ fUa g'k ]h\'h\Y'dYfa ]gg]cb'cZh\Y'fY'Yj Ubh7cbj Ybcf"

: cf'XYHJ]g'cb'\ck 'hc'Udd`md`YUgY'WcbHJWh\Y': UW'\hmK  $cf_'=bhY[fUhYX'@YUfb]b['I b]h.': <math>\underline{5GGI}$ K =4 i bqk "YXi "Ui "

#### 7ci fgY @YUfb]b[ Ci hWca Yg

%" K f]hY 'Ub 'Wf]h]WU`! UbU`mg]g! VUgYX`YggUmž'Yj ]XYbWY`cZUWf]cb`fYgYUfWX
&" 6Y`]bj c`j YX`]b`Ub`UWf]cb`fYgYUfWX`dfcYWh
' " 7 ca d`YhY`U`Vi g]bYgg`cf]YbhYX`hUg\_\_``
( " I bXYfghUbX`h\Y`XmbUa ]Wg`cZk cf\_]b[ `k ]h\]b`cf[ Ub]gUh]cb

### HYUWX]b[ 'GhfUhY[]Yg'

HYUW ]b[ GlfUhY[ ]Yg UbX F Uh]cbUY.

 $\label{thm:continuity} $$H'Y'dfUWfWU''j cWUfjcbU''d'UW'a Ybh''gWXYXi 'Y']g'gi ddcfhYX'Vm'U'fYUX]b['dfc[fUa''h\UhYI'Ua]bYg'X]ZZYfYbh UddfcUWXYg'hc'h\Y'gh' XmcZcf[Ub]gUfjcbg'fh\Y]f'ghfi WhifYgž'\(\frac{1}{2}\) bWfjcbg'UbX''dc']\(\frac{1}{2}\) fygY']ggi Yghc'h\Y'd'UW'a Ybh'YI dYf]YbW'''$ 

Ghi XYbhg'k]``gdYbX'%\$) 'k cf\_]b['\ci fg'Uh'U'\cghcf[Ub]gUh]cb'UbX'k]``\Uj Y'h\Y]f'k cf\_'Yj U`i UhYX'Vm'h\Y\cghcf[Ub]gUh]cb'''\b'\Y]f'k cf\_'Yj U`i UhYX'Vm'h\Y\cghcf[Ub]gUh]cb'''\b'\X]h\cb''ghi XYbhg'k]``Wta d'YhY'U'XU]`mX]UfmUbX'Ub'YggUmVUgYX'cb'h\Y]f'UbU'mg]g cZh\Y'cf[Ub]gUh]cb'''H\Ymk]``'U'gc'Wta d'YhY'Ub'Yj U`i Uh]cb'cZh\Y]f'k cf\_d'UWY'YI dYf]YbWY'Ug'ZYYXVUW\_hc h\Y'Wti fgY'Wtbj Ybcfg

H\]g`Wci fgY`]g`U`fYUX]b[ `dfc[ fUa `UbX`gh XYbhg`UfY`YI dYWhYX`hc`VY`]bXYdYbXYbh'UbX`gY`ZXfYWhYX`YUfbYfg"`7 ci fgY`Wcbj Ybcfg`a YYhigh XYbhg`cb`Ub`Ug!bYYXg`VUg]g"

6YZcfY`VY[]bb]b[`Ub`j cWUh]cbU``d`UWYa Ybhz`h\Y`gWcdY`cZU`ghi XYbhfijj cWUh]cbU``d`UWYa Ybh`UWfj ]h]Yg`k]``VY`U[fYYX`k]h\Y`\cghcf[Ub]gUh]cb"`Ghi XYbhg`k]```\Uj Y`U`ghfcb[`jc]WY`]b`h\YgY`]b]h]U``bY[ch]Uh]cbg`UbX k]```VY`Ug\_YX`hc`g][bU``h\Y]f`U[fYYa Ybh'`5`ghi XYbh'Wca a YbW]b[`jcWUh]cbU``d`UWYa Ybh'k cf\_'k]```VY Ugg][bYX`U`\cghgi dYfj]gcf`hc`a UbU[Y`h\Y]f`gdYW]ZWj cWUh]cbU``d`UWYa Ybh'UWfj]h]Yg"

 $Ghi XYbhg`UfY`Ybfc``YX`]b`<IAG`&\$\$\$`UZhYf`U`\cghcf[Ub]gUh]cb``\Ug`VYYb`gcifWX`UbX`h\Y`7cifgY 5WUXYa]W\Ug`YbXcfgYX`h\Y`d`UWYaYbh'`KY`k]```VY`ig]b[`AccX`Y`hc`giddcfh'h\Y``YUfb]b[`UbX`hYUW\]b[UW]j]h]Yg`cZh\]g`WcifgY"$ 

5ggYgga Ybh' . <cgh'9j U`i Uh]cb

GhUfhXUhY. Bch5dd`]WUV`Y

**@Yb[h**\. B#5

**8YHJ]`g**. `H\]g`XcYg`bchHJ\_Y`]bhc`Wcbg]XYfUh]cb`h\Y`k cf\_d`UWY`Wca dcbYbH'`H\]g`]g`h\Y`Z]bU``UggYgga Ybh HJg\_`Zcf`h\]g`Wci fgY": YYXVUW\_`Zca `\cghigi dYfj ]gcf"

Hi fb]hjb gYhjb[. H\]g ]g bchU Hi fb]hjb Ugg][ ba Ybh

5ggYgga Ybh ( . Cf[ Ub]gUh]cbU YggUm

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. &\$\$\$ k cfXg

**8YHJ]`g**. ``%cZ&T :: ]bU``YggUmg`&\$\$\$`k cfXg`K f]HYb`ZYYXVUW\_

 $\label{thm:continuous} \begin{tabular}{ll} Hi & fb & fb & gYM &$ 

### 5 https://bxubwww.Fyei ]fya Ybhg

H Y f Y U

# 7ci fgY GWX YXi `Y

#### J ]Yk 'WUgg'ha YhUV'Y

### H]a YHJV`Y

8UHY	Hmd Y	7 cbh/bh
±blYfbg\]d		H\YfY`UfY`bc`fY[i`Uf`WUggYg`]b`h\]g`WtifgY"`9UW\ ghiXYbhaYYhg`h\Y`5WUXYa]W7cbjYbcf`hc`X]gWigg h\Y`ZcWig`cZh\Y]f`UWUXYa]Wkcf_'h\Uh]g`WcgY`m `]b_YX`hc`h\Y]f`]bhYfbg\]d"

# FYgci fWfg

### DfYgWf]VYX F Ygci fWYg

#### FYWca a YbXYX FYgci fWYg

FYZYf'hc'h\Y'<1 AG&\$\$\$``Y[Ubhc'`]b\_"

### 7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

5```ZYYXVUW\_`Zfca `ghi XYbhg`]g`j U`i YX"'H\Y`Wti fgY`Wt!cfX]bUhcf`gYY\_g`]bZcfa U``ZYYXVUW\_`Zfca `YUW.

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

Image: Ybwb: bh/f'u'dfcv'ya k \yb'uhh/a dh/b[ 'hc'gi va ]hmci f'ugg][ ba Ybhh\fci [ \ 'Hi fb]h/bž'd'YugY

HY'Yd\cbY'9| h/fbu''Gi ddcfhcb'-', ) '' ' ' %cf'Ya U] 'h\Ya 'cb'Yl h/fbu'h/hgi ddcfh4 i bgk "YXi "Ui "'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'\\$\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ'' Image
UfY'i bUV'Y'hc'gi va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\ 'Hi fb]h/b'mci 'a UmUdd'mZcf'Ub'Yl h/bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h/W\_Yhbi a VYf'Zfca '9| h/fbU''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'YY] UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj ]XYbW''hc'gi ddcfhmci f'Yl h/bg]cb'Udd']\WJh/jcb'' Image 'Ya U]''9| h/fbU''Gi ddcfhmci 'k ]'`
Ui hca Uh/WJ'`mfYW']j Y'U'h/W\_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k ]'`'bYYX'hc'gdYW/ZWJ'`mUg\_'Zcf'cbY''
Hi fb]h/b'U'gc'dfcj ]XYg'i dXUh/g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk ]hYf''

; YbYfU``mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\W)``mj ]U'Y]h\Yf'Hi fb]hjb'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]``'VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\ U`hYfbUhj Y'gi Va ]gg]cb'XYHJ]`g''

cfi]bZcfa Uh]cbicbi\ckihcigi Va ]hUgg][ ba Ybhgicbi]bYij ]UiA ccXiY.i\hdg.#gh XYbh'i bgk "YXi "Ui #\ck! gi Va ]hUgg][ ba Ybha ccXiY

# $5\,WUXYa\,W< cbYghmUbXDU[\,Uf]ga$

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=iWUbiHU\_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'i

- i bXYfgHUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbhUhI BGK
   VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hz'I BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5VWWdhUV`Y'I gY'cZ IBGK =7 HF Ygci fWrg Dc`]Wh

# 5 WUXYa ]W±bZcfa Uhjcb

: cf'YggYbhJU`gh XYbh]bZcfa UhJcb'fY`UhJb['hc.

• fYei YghgʻZcfʻYl hYbg]cb/