CVEN9407

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CVEN9407 // Term 2, 2022 // published at 25-05-2022 © UNSW Sydney, 2022

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7cifgY[·]8YHJ]`g

I b]hg`cZ'7 fYX]h'*

Gi a a UfmcZh\Y'7ci fgY

A cXY``]b['lfUbgdcffUlf]cb'XYa UbX'UbX'gUZYlm/U'VfcUX'fUb[Y'cZYWcbca Ylf]Wa cXY``]b['lfWXb]ei Yg'UbX']lg Udd`]WUlf]cb'rc'lfUbgdcffUlf]cb'gmglYa g'k]``VY'Wcbg]XYfYX/gdYW]Z]WYa d\Ug]g'k]``VY'd`UWYX'cb'Yglf]a Ulf]cb cZh\YgY'a cXY`g'UbX'h\Y]f'i gY'Zcf'ZcfYWUglf]b['UbX']bhYfdfYlUlf]cb'cZfYgi `lg/'lfUbgdcffUlf]cb'XUlfUž'UbU`mg]g UbX'a cXY``]b[']bWi X]b['Wcbg]XYfUlf]cbg'cZXUlfU'gci fWfgž'Yffcfgž'lf]a Y'gYf]Yg'UbU`mg]gžghcWXUglf]Wa cXY`g UbX'Yl hYbg]cbg'rc'g]a i `Ulf]cb'UbX'cdh]a]gUlf]cb']b'lfUbgdcffUlf]cb'gmghYa g"

7 ci fgY⁻5]a g

CVYWjYCZh\YWcifgY`]g`hc`]adUfhUXjUbWX`_bck`YX[Y`]b`ffUbgdcfhacXY``]b[`k]h\UZcWg`cb

5ggYgga YbhgʻfhYghgžYI Ua]bUhjcbgžUgg][ba YbhgŁ

- 8 Ya cbgHfUHY mci f _bck `YX[Y 'UbX g_]``g
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5XX]h]cbU``XYHJ]`g

7 ca dfY\Ybg]j Y i bXYfgHJbX]b[cZVUg]WgHJh]gh]Wg UbX dfcVUV]`]h]Yg

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I bXYfgHJbX]b['UVci hH\Y'VUg]WUggi a dh]cbg'VY\]bX``]bYUf'fY[fYgg]cb'a cXY`g"

Ghi XYbhgʻk]```VYʻUggYggYXʻVUgYXʻcbʻh\YʻUVWV fUWniUbXʻj U`]X]hnicZh\Y]fʻgi Va]hhYXʻgc`i hjcbgʻhcʻh\Y ei Yghjcbg"

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5ggYgg]b['gh XYbhgfi_bck `YX[Y'UVci ha cXY`g'Zcf'bcb!Wcbh]bi ci g'XYdYbXYbhj Uf]UV`Yg

5`\UbXg`cb`dfcYWhik]h\`gmbh\Yg]gYX`XUhU

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8i Y'XUHY. '9I Ua g'k YY_

7 cj Yf]b['U```hcd]WWcj YfYX`]b`h\Y`Wci fgY"

H\Y'dUgg'a Uf_`]b'h\]g'Wci fgY']g') \$1 _`cj YfU``ž\ck Yj Yfž'gh XYbhg'a i ghgWcfY'Uh`YUgh(\$1 _`]b'h\Y'Z]bU` YI Ua]bUh]cb']b'cfXYf'hc'ei U`]ZmZcf'U'DUgg']b'h\]g'Wci fgY'fKci V`Y'\i fX`YŁ"

5HYbXUbW/FYei]fYaYbhg

Ghi XYbhgʻUfYʻghfcb[`mYbWci fU[YX'hcʻUhhYbX'U```WUggYgʻUbX'fYj]Yk ``YWhi fYʻfYWcfX]b[g"

7 ci fgY GWX YXi `Y

8iY'hc'U'diV`]W\c`]XUmcb'h\Y'% h\`cZ>ibYžh\YfY`]g'bc']b!dYfgcb'hYUW\]b[`cb'h\]g'gdYWJZ]Wk YY_žUbX'h\Y WcifgY'aUhYf]U'g'k]``VY'UjU]`UV'Y'cb`]bY'Zcfincif'fYj]Yk "'5``ch\Yf'k YY_g'UfY'cZYfYX']b'U'\m\f]X'acXY"

5 HUVY cZYW i fYgʻUbX k cf_g\cdgʻcfʻdfUWjWU`WUggʻhcd]WgʻZcfYUW k YY_ž]bX]WUHjb[`H\Y`bUa Y`cZH\Y YW i fYf`]bj c`j YX`fk \YfY`a i `Hjd`Y`YW i fYfgʻHYUW.]b[`]b`H\Y`Wci fgYŁzcb`]bY`UWHj]]HYgžgi W.`UgʻX]gW gg]cb Zcfi a gz`UbX`fY`Yj UbhfYUX]b[gʻZca `HYI H/cc_g`UbX`ch\Yf`fYZYfYbWFa UHYf]U``]XYbHjZ]YX`ZcfH\Y`Wci fgY"

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		FYj]Yk`cZgHUh]gh]Wg`UbX`dfcVUV]`]h]Yg
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Gi Va]gg]cb cZ5ggYgga YbhHUg_g

D`YUgY`fYZYf`hc`h\Y`A ccX`Y`dU[Y`cZh\Y`Wci fgY`Zcf`Z fh\Yf`[i]XUbWY`cb`UggYgga Ybhigi Va]gg]cb"

I BGK `\Ug`U`gHUbXUfX``UhY`gi Va]gg]cb`dYbU`hmcZ

)ı 'dYf'XUmž'Zcf'U``UggYgga Ybhg'k \YfY'U'dYbU`hm'Udd`]Ygž'WUddYX'Uh'Z]j Y'XUmg'f%&\$'\ci fgŁz'UZYf k \]W\'U'ghi XYbh'WUbbchigi Va]h'Ub'UggYgga Ybhž'UbX'bc'dYfa]hhYX'j Uf]Uh]cb"

5WUXYa]W<cbYghmUbX D`U[]Uf]ga

6Yk UfY**5b*Ugg][ba Ybhh\Uh]bWi XYg*d*U[]Uf]gYX*a UhYf]U**k]***fYWY]jY*U*\$i=***U]*žUbX*ghi XYbhg*k \c d*U[]Uf]gY*a UmZu]**h\Y*Wci fgY***Ghi XYbhg*k \c*d*U[]Uf]gY*UfY*U*gc**]UV*Y*hc*X]gW]d*]bUfmUWf]cbž*]bWi X]b[YI Wi g]cb*Zfca *Ybfc*a Ybh

D`U[]Uf]ga `]g`h\Y`i gY`cZUbch\Yf`dYfgcb'g`k cf_`cf`]XYUg`Ug`]Zh\Ymk YfY`mci f`ck b"`K \Yb`]h]g`bYWyggUfmcf XYg]fUV`Y`hc`i gY`ch\Yf`dYcd`Y'g`a UhYf]U``mci `g\ci `X`UXYei UhY`mUW_bck `YX[Y`k \cgY`k cfXg`cf`]XYUg`h\Ym

5WUXYa]W=bZcfaUh]cb

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:]bU`YI Ua g`]b`H&`&\$&&`k]``VY`\Y`X`cb`]bY`VYfk YYb`%&f\`!`&) f\`5i [i gh&\$&&`]bWi g]j Yž'UbX gi dd`Ya YbfUfm`YI Ua g`VYfk YYb`) f\`!`-f\`GYdfYa VYf`&\$&&`]bWi g]j Y"`Nci `UfY`fYei]fYX`fc`VY`Uj U]`UV`Y`cb f\YgY`XUfYg"`D`YUgY`Xc`bchfc`a U_Y`UbmidYfgcbU``cf`ffUj Y``UffUb[Ya Ybfg`Xi f]b[`f\]g`dYf]cX"`

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