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- ' " I bXYffU_Y`VUg]Wgi fj YmWca di HUfjcbgʻZca ʻfUk ʻZ]Y`X`cVgYfj Ufjcbgʻhcʻgi ddcfhUʻfUb[Y`cZgi fj Ym]b[UbX`Yb[]bYYf]b[`Udd`]WUfjcbgʻgi W. 'Ug``Yj Y``]b[`UbX`HYffU]bʻfYdfYgYbHUfjcbžUfYUʻUbX`j c`i a Y WU`W`UfjcbgžHfUj Yfq]b[`UbX`WcbgHfi WfjcbʻgYhci H'
- ("5dd`mh\Y`h\YcfmVY\]bX`h\Y`j Uf]ci g`gi fj Ym]b[`UbX`[YcgdUh]U``hYW\b]ei Yg`dfYgYbhYX`]b`h\]g`Wci fgY UbX`Wf]h]WU``mUggYgg`h\Y`ei U`]hmcZ[YcgdUh]U``XUhU"

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