

## **AERO4620**

8 mbUa ]Wg cZ5YfcgdUWY JY\]WYgžGmghYa g UbX 5j ]cb]Wg

HYfa 'C bY''##'&\$&%

## 7ci fgY 8YHJ] g

#### 7 fYX]hDc]bhg\*\*

#### Gi a a UfmcZh\Y 7ci fgY

Dck Yfžra UggʻUbXʻ]bZcfa UhjcbʻhfUbgZYf": `i ]X]Wža YWXUb]WU``UbX`Y`YWff]WU``gmghYa gʻ]bʻUYfcgdUWYʻj Y\]WWg/Ybj ]fcba YbhWcblfc`"5j ]cb]WgʻUbX`UXj UbWYX`U]fWfUZhgmghYa g/Wca di hYf!U]XYX'j Y\]WYʻa UbU[ Ya Ybh'5j ]cb]WgʻIbhY[ fUhjcb"5]fVcfbY`gYbgcfg"BUj ][ Uhjcb"`GHUV]`]hmUbX`Wcblfc``gmghYa g" 7 cW\_d]hYbj ]fcba Ybh'`GHUhjWUbX`XmbUa ]WgHUV]`]hmcZUha cgd\Yf]Wj Y\]WYg": `][ \hiWcblfc`"<UbX`]b[ `UbX Zmjb[ `ei U`]hYg"

#### 7 ci fgY 5]a g

 $8 \ mbUa \ [Wg'cZ5YfcgdUW'JY\]WYgž'GmghYa g'UbX'5j \ ]cb]Wg']g'U'\][\ Yf'`Yj Y``5YfcgdUW'`9b[\ ]bYYf]b[\ 'Wci fgY]b'k \ ]WhYz'UbX'YI hYbXYX''$ 

H\]g`Wci fgY`ZcW gYg`cb`\ck 'h\Y`U]fWfUZhVY\Uj Yg`Ug`U'hJa Y!XYdYbXYbhGMGH9A "'=hU]a g`hc'hYUW\`mci

WUggfcca 'h/UW\]b['k]``'VY'gi ddcfhYX'Vm`YWh fY'bchYg'Uj U]`UV`Y'cb`]bY"'H\Ymk]``'WcbhU]b'Vf]YZci h]bYg'cZh\Y'a cgh']a dcfhUbhdc]bhg'Ug'k Y``'Ug``]b\_g'hc'h\Y'a cfY'XYhU]`YX'gci fWrg"

#### 5XX]h]cbU`7ci fgY +bZcfa Uh]cb

 $H\setminus [g^*]g^*U^*ib]hcZWfYX]hflc7EWcifgY^UbX^]bjc^jYg^gYjYb^\cifg^dYf^kYY_fh#kEcZZUWf!hc!ZUWf^WcbhUWf^$ 

 $\label{thm:condition} $$HY'bcfa\ U''k\ cf_cux'YI\ dYWfuhcbg'cZU'ghi\ XYbh'ufY'UddfcI\ ]a\ UhY'm'&) '\ci\ fg'dYf'hYfa\ 'Zcf'YUW\'I\ C7ž\ ]bWi\ X]b[\ 'WUgg'Wcbh'uWfi\ci\ fgž'ch\Yf''YUfb]b[\ 'UWhjj\ ]h]Ygž'dfYdUfUhjcb''UbX'hJa\ Y'gdYbh'cb''U'''UggYggUV'Yk\ cf ''$ 

Mci 'g\ci `X'U]a 'hc'gdYbX'U\ci h'\&'\#k 'cb'h\]g'Wci fgY"'H\Y'UXX]h]cbU`'h]a Y'g\ci `X'VY'gdYbh]b'a U\_]b[ gi fY'h\Uhmci 'i bXYfghUbX'h\Y'`YWh fY'a UhYf]U'ž'Wca d`Yh]b[ 'h\Y'gYhUgg][ ba Ybhgž'\I fh\Yf'fYUX]b[ ž'UbX fYj ]g]b[ '\Icf'UbmYl Ua ]bUh]cbg"

: cf`YUgY`cZa UbU[Ya Ybhžh\Y`Wci fgY`]g`cf[Ub]gYX`]bhc`h\fYY`gYdUfUhY`dUfhg.`5YfcgdUWY`GmghYa gž 5j ]cb]Wg`UbX`: `][\h'8 mbUa ]Wg/h\Ymk ]```Zcfa `A cXi `Yg`5ž6`UbX`7 `fYgdYWfj Y`m'`A cXi `Y`5`k ]``fi b`]b K YY\_g`%-'' `UbX`A cXi `Yg`6`UbX`7 `]b`K YY\_g`(`-'%\$"`\b`UXX]h]cbž'h\YfY`]g`Ub`]bX]j ]Xi U``Z][\h'g]a i `Uh]cb YI YfW[qY"

H\Y'5YfcgdUW'GmghYa g'dUfhXYU\g'k]h\rh\Y'gc!WU\YX'U]fZfUa Y'gmghYa g'Ug'k Y\``'Ug'h\Y]fYZZYWicb U]fWfUZhg'dYfZcfa UbW'"'H\Y'5j ]cb]Wg'gY[ a Ybhgh X]Yg'U]fWfUZhY\YWfcb]WgmghYa g'Ug'k Y\``'Ug'ch\Yf gmghYa g'h\UhX]fYWhm]bhYfZJW'k ]h\rangle 'Y\YWfcb]Wg"'H\Y': \cdot \cdot ]\kg'Wcj Yfg'X]ZZYfYbhUgdYWg'cZ'U]fWfUZh ghUY]\]hm\UbX'h\Y'dUfUa YhYfg'h\UhUZYWh]h''H\Y'k]bX'hi bbY\`YI dYf]a YbhXYa cbghfUhYg'h\Y\'`cb[]hi X]bU\cdot ghUV]\]hm\ubx'i bXYfghUbX]b[ 'cZk \]W\cdot ]g'Wfi W]U\cdot Zcf'Z][\hWcbfc\cdot gmghYa g'' \ddot \udy Ug'UbX'5j ]cb]Wg'a cXi 'Yg'': ]bU\cdot m\ubx'h\Y'Z][\hg]a i 'Uh]cb'Yl dYf]a YbhXYa cbghfUhYg'h\Y cdYfUhYg'h\Y cdYfUhYg'b\Y g'h\Y Uf]ci g'bUj ][ Uh]cb'UbX'Wca a i b]Wh]cb'gmghYa g''

59FC(\*&\$`]g`Ub`]a dcffUbhghYdd]b[`ghcbY`]b`UYfcgdUW'Yb[]bYYf]b[`YXi WUhjcb"'H\Y`\_bck`YX[Y`UWei]fYX Xi f]b[`h\]g`Wci fgY`]g`X]fYWhmUdd`]WUV`Y`hc`h\Y`[fci d`XYg][b`]b`59FC(%%\$"`Cb`h\Y`ch\Yf`\UbXžAcXi`Y`7cZh\]g`Wci fgY`X]fYWhmfY`UhYg`hc`h\Y`dYfZcfa UbW'dUfhcZ59FC'\*\*\$/Uhh\Y`gUaY`hJaY`h\Y`ghUV]`]hm UbU`mg]g`cZZm]b[`j`Y\]WYg`dfYgYbhYX`]b`h\]g`acXi`Y`]g`VUgYX`cb`aYh\cXg``YUfbYX`]b`AA5B'&\$\$`@]bYUf GmghYag`UbX`7cbfc`"'H\Y``Uf[Y`aU`cf]hmcZh\]g`WUgg`\Ug`VYYb`]bjc`jYX`]b`Z][\hiYl dYf]aYbhg`h\Uhdfcj]XYU'Wfi WJU``]b\_'VYhkYYb`h\Y`h\YcfYhJWU`\_bck`YX[Y`[U]bYX`Xi f]b[`h\Y`WUgg`hJaY`UbX`fYU``Z][\hig]h`Uhjcbg" Gh`XYbhg`UfY`U`gc`UV`Y`hc`cVgYfjY`h\Y`Z bWhjcb]b[`cZgmghYag`Zci bX`]b`; YbYfU``5j`]Uhjcb`U]fWfUZh'`5```h\YgY WcadcbYbhg``Uf[Y`mWcbhf]Vi hY`hc`XYjY`cd]b[`bYWfggUfmYb[]bYYf]b[`g\_]``g`UbX`\_bck`YX[Y"

## 5ggYgga Ybh

<1 F8@9 F9E1 ≠9A 9BH

±b cfXYf hc dUgg h\Y Wci fgYžmci 'U`gc \Uj Y hc cVhU]b 'U hchu` cZUh`YUgh) \$i f&& a Uf\_gŁZcf h\Y A cXi `Y 7. HYgh& fl&i ŁŽ @UV fYdcfhfl%( i Ł'Ž A cXi `Y 7 dUfhcZh\Y ZbU``YI Ua fl% i Ł"

#### 5ggYgga YbhHUg\_g

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UHY	Gh XYbh@YUfb]b[ Ci hWca Ygʻ5ggYggYX
: ]bU`YI Ua '	(*	Bch5dd`]WUV`Y	%ž'&ž'' ž'(
HYghg.	(\$1	Bch5dd`]WUV`Y	%ž'&ž'' ž'(
@UV F Ydcfhi	%( ।	&\$#\$(#&\$&%`%%)\$`DA	%ž <sup>:</sup> (

5ggYgga Ybh8YhJ]`g

5ggYgga Ybh'% : ]bU`Yl Ua

GhUfhiXUhY. Bchi5dd`]WUV`Y

8YHJ]`g.

: ]bU`YI Ua 'hYgh]b[ 'h\Y'Ybh]fY'A cXi Y'6'Ug'k Y``'Ug'XmbUa ]WghUV]`]hm'

5ggYgga Ybh'& 'HYghg

GhUfhXUhY. Bch5dd`]WUV`Y

8 YW] g.

HYgh%cb h\Y Ybh]fY A cXi Y 5 fl \$1 \text{2"HYgh&cb ghUh]WghUV]`]hmfl&i \text{2"}

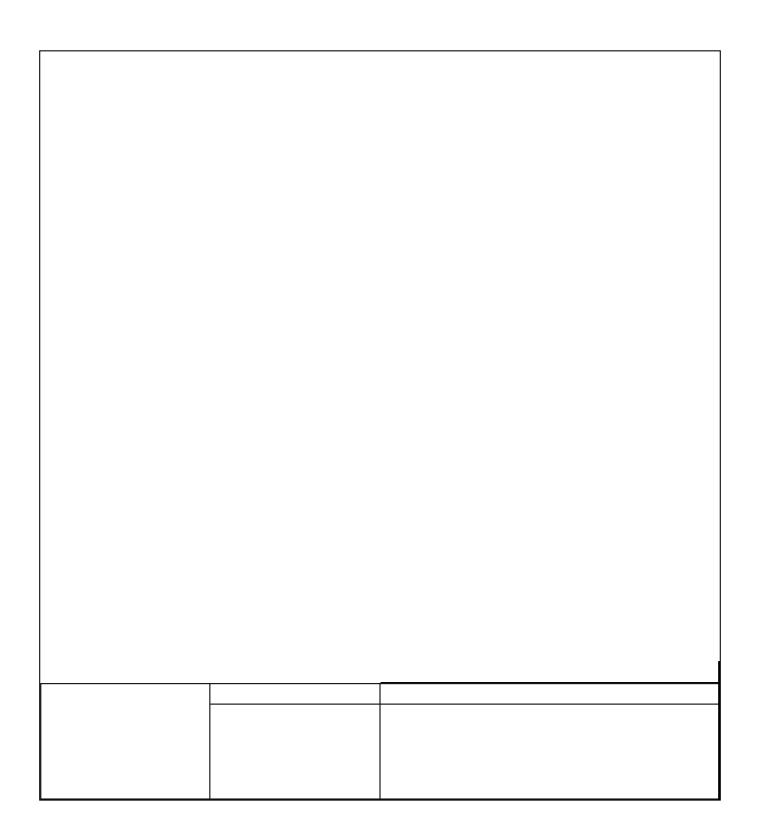
5ggYgga Ybh' . @UV F Ydcfh

GhufhXuhY. Bch5dd`]WUV`Y

8 YW] g.

K ]bX'hi bbY`'a YUgi fYa Ybhg'k ]``'VY'i gYX'Zcf'UggYgg]b[ 'h\Y'`cb[ ]hi X]bU`'ghUV]`]hmdUfUa YhYfg"

 $\label{thm:limit} \begin{tabular}{ll} Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h]b "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h]h "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h "UbX"gh XYbhg"Xc "bchgYY"Hi fb]h "UbX"gh XYbhg"Xc "bchgYY "hi fb]h "UbX"gh XYbhg"Xc "bchgYY "bchgy XYbhg"Xc "bchgYY "bchgYY "bchgy XYbhg"Xc "$ 



#### FYgci fW/g

#### DfYgWf]VYX F Ygci fWYg

H\YfY`]g`bc`hYl hVcc\_Zcf`h\Y`Wci fgY"`Dck YfDc]bhg`]XYg`k ]```VY`Uj U]`UV`Y`cb`A ccX`Y`Zcf`A cXi `Yg`5`UbX`6``YWfi fYg`Vi hghi XYbhg`UfY`Yl dYWYX`hc`i gY`j Uf]ci g`gci fWfg"

#### FYWca a YbXYX FYgci fWfg

5j ]Uh]cb'H\Ycfm'7 YblfY'flA Y`Vci fbYž'J ]WŁ'&\$\&UZin[ YbYfU`\_bck `YX[ Y`UbX'UYfcXmbUa ]Wg'Zcf'h\Y 7 5G5'DD@UbX'7 D@XUmJ: F'gm`UVi g"ž<i bh]b[ XU`Yž'J ]W.''5j ]Uh]cb'H\Ycfm'7 YblfY

7c``]bgcbžF"'-''+blfcXi Wf]cb'hc'5j ]cb]\\gamma''z'\\ghYX"z'\@cbXcb/BYk '\Mcf\_.'7\Uda Ub'/ '<U``

5 aa] ł? žHžł 8 (YZf 6 k`S\_ [Ue B d)` U[b We ł 3 d a  $^{\prime}$  B g T (eZ W deł G = ł #++)

Bai WdBa[fe^{VWe Xad?aVg^We 3 S`V 4

? aaV₩

## Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

#### 5ggYgga Ybhgi Va ]gg]cb UbX a Uf\_]b[ Wf]hYf]U

G\ci`X'h\Y'\\ci`fgY'\Uj Y'Ubmbcb!Y`Y\\fcb]\\UggYgga Ybhigi Va ]gg]cbž'h\YgY'g\ci`X'\Uj Y'U'g\\bXUfX G\\cc``\\cij Yf'g\YYh'

 $5 ```gi Va ]gg]cbg`UfY`YI dYWYX`hc`VY`bYUh`UbX`WYUf`mgYhci h'`Mci f`fYgi `hg`UfY`h\Y`d]bbUWY`cZU```mci f`\UfX k cf_'UbX`g\ci `X`VY`hfYUhYX`k ]h\`Xi Y`fYgdYWf`DfYgYbh]b[ `fYgi `hg`WYUf`m[ ]j Yg`h\Y`a Uf_Yf`h\Y`VYgh'W\UbW' cZi bXYfghUbX]b[ `mci f`a Yh\cX/Yj Yb`]Zh\Y`bi a Yf]\W\``fYgi `hg`UfY`]b\\cffY\Wf$ 

 $\label{thm:condition} $$ \ensuremath{\mathsf{U}} = \ensuremath{\mathsf{U}} =$ 

I BGK 'bck '\Ug'U': <u>]hhc'G]h#Gi Va ]hffi 'Y</u>ž'k \]W\ 'a YUbg'h\Uh]Zmci 'UhhYa dh'Ub'YI Ua 'cf'gi Va ]h'U'd]YW''cZ UggYgga Ybhž'mci 'UfY'XYWUf]b[ 'mci fgY`ZZ]hYbci [\'hc'Xc'gc'UbX'WUbbch`UhYf'Udd`mZcf'GdYW]U` 7 cbg]XYfUh]cb"

: cf`XYhJ]`g`cZUdd`m]b[ 'Zcf`GdYVJU``7 cbg]XYfUh]cb`UbX`WcbX]h]cbg'Zcf`h\Y`Uk UfX`cZgi dd`Ya YbhUfm UggYgga Ybhž'd`YUgY`gYY`h\Y`]bZcfa Uh]cb`cb`l BGK 'g`<u>GdYVJU``7 cbg]XYfUh]cb`dU[Y</u>"

D`YUgY'bchY'h\Uhgh XYbhg'k]``bchVY'fYei]fYX'hc'dfcj]XY'UbmXcW a YbhUfmYj]XYbW'hc gi ddcfhUVgYbWg'Zfca 'UbmWUggYg'a]ggYX'VYWUi gY'cZ'7CJ=8!% 'di V`]W\YU'h\ 'a YUgi fYg'gi W\'Ug

## 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

 $\label{thm:continuous} IBGK ``Ug`Ub`cb[c]b[`Wcaa]haYbhhc`ZcghYf]b[``U`W``hifY`cZ`YUfb]b[`]bZcfaYX`VmUWUXYa]W]bHY[f]hm'`5``IBGK `ghiXYbhg`UjY`U`fYgdcbg]V]`]hmhc`UX\YfY`hc`h\]g`df]bW]d`Y`cZUWUXYa]W]bHY[f]hm'D`U[]Uf]gaibXYfa]bYg`UWUXYa]W]bHY[f]hmUbX`]g`bchhc`YfUhYX`UhIBGK "`B'SY[Sde_SfG@EI[eVW{`WSege[YfZW_aXSekagdai`ž$ 

D`U[]Uf]ga `]g`U`lmdY`cZ]bhY``YWi U``lh\YZh''=i\WUb`HU\_Y`a UbmZcfa gžZfca `XY`]VYfUhY`W\YUlf]b[ 'lc`U\W]XYbHU``m Wcdm]b[ 'Zfca `U`gci fW'k]h\ci hUW\_bck `YX[Ya Ybh''I BGK `\Ug`dfcXi WYX`U`k YVg]hY`k]h\`U`k YU`h\`cZ fYgci fW'g`lc`gi ddcfhighi XYbhg`lc`i bXYfghUbX`UbX`Uj c]X`d`U[]Uf]ga žij ]g]h 'ghi XYbh'i bgk "YXi "Ui #d`U[]Uf]ga\_" H\Y`@YUfb]b[ '7 YbhY`Ugg]ghg`ghi XYbhg`k]h\`i bXYfghUbX]b[ 'U\WXYa]W]bhY[f]hmUbX`\ck 'bchhc'd`U[]Uf]gY" H\YmU`gc`\c`X`k cf\_g\cdg`UbX`\Wb`\Y`d`ghi XYbhg`cbY!cb!cbY"

Mci 'UfY'U'gc'fYa ]bXYX'h\UhWUfYZ ``h]a Y'a UbU[ Ya Ybh]g'Ub']a dcftUbhdUfhcZgh XmUbX'cbY'cZh\Y ]XYbh]Z]YX'WUi gYg'cZd`U[ ]Uf]ga ']g'dccf'h]a Y'a UbU[ Ya Ybh'Gh XYbhg'g\ci 'X'U``ck 'gi Z]W]Ybhh]a Y'Zcf fYgYUfW\žXfUZh]b[ 'UbX'h\Y'dfcdYf'fYZYfYbW]b[ 'cZgci fW/g']b'dfYdUf]b[ 'U```UggYgga YbhHUg\_g''

₹d`U[]Uf]ga i]gʻZci bXi]bimci fik cf\_ik \Ybimci 'UfYi]bʻZ[fghmYUfžimci fi`YWi fYfik]``cZYfimci 'Ugg]ghUbWYihc
]a dfcj Yimci fi'UWUXYa]Wg\_]``g'''H\Yma UmUg\_imci ihci`cc\_'Uhigca Yicb`]bYifYgci fWygžiUhhYbXih\Yi@YUfb]b[
7 YbhfYžcfigca Yh]a YgifYgi Va]himci fik cf\_ik]h\h\YidfcV`Ya iZ[l YX'''< ck Yj Yfia cfYigYf]ci gi]bghUbWygi]biZ[fgh
mYUfžigi W\ugighYU`]b[iUbch\Yfighi XYbhgik cf\_icfidUm]b[igca YcbYihciXcimci fik cf\_žia UmVYi]bj Ygh][UhYX
i bXYfih\YiGhi XYbhA]gWcbXi WhDfcWYXi fYg''

F YdYUHYX'd`U[]Uf]ga `fYj Yb`]b`ZjfghmYUfłžd`U[]Uf]ga `UZHYf`ZjfghmYUfžcf`gYf]ci g`]bgHUbWYgža Um'U`gc`VY ]bj Ygh][UHYX`i bXYf`h\Y`Ghi XYbhA ]gWcbXi WhDfcWYXi fYg"`H\Y`dYbU`h]Yg`i bXYf`h\Y`dfcWYXi fYg`WUb`]bWi XY U`fYXi Whcb`]b`a Uf\_gž`ZU]`]b[`U`Wci fgY`cf`Zcf`h\Y`a cghgYf]ci g`a UHHYfg`fi]\_Y`d`U[]Uf]ga `]b`Ub`\cbci fg h\Yg]gŁYj Yb`qi qdYbq]cb`Zfca `h\Y`i b]j Yfq]mm'`H\Y`Ghi XYbhA ]qWcbXi WhDfcWYXi fYg`UfY`Uj U]`UV`Y`\YfY.

kkk"[g"i bgk"YXi"Ui #dc]Wn#XcWa Ybhg#ghi XYbha ]gWcbXi WhdfcWYXi fYg"dXZ

#### a dcfhUbh'@]b\_g

- A ccX`Y
- <u>@UV:5\W\/aa</u>
- < YU`h\ 'UbX'GUZYhm
- <u>7 ca di h|b[ : UW|^]h|Yq</u>
- Gh XYbhF Ygci fWg
- 7 ci fgY 'Ci h]bYg
- 9b[]bYYf]b['Gh XYbhGi ddcfhGYfj]\Wg:7YblfY
- A U YfadUW
- I BGK 'H]a YHUV'Y
- I BGK '< UbXVcc
- LBGK 'A YWXUb]WU``UbX'A Ubi ZUWh f]b[ '9b[ ]bYYf]b[
- <u>9ei ]hUV`Y`@YUfb]b[ 'GYfj ]WYg</u>

#### a U[Y'7fYX]h

GmbYf[]Yg^]b^GcibX^&\$%\*

#### 7F = 7CG

7F = 7 C G 'Dfcj ]XYf '7 c XY. '\$\$\$-,;

#### 5W\_bck `YX[ Ya YbhcZ7ci blfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb U : W ghcX]Ubg : cZh, Y ``UbXg : cb : k \ ]WX : I B G K ? Ybg]b[hcb : WUa di g : ]g ``cWUhYX''$ 

# 5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

Dfc[fUa '±bhYbXYX'@YUfb]b['CihWca Yg	
?bck `YX[Y'UbX'g_]```VUgY	
D9%"%7cadfY\Ybg]jYžh\YcfmVUgYX`ibXYfghUbX]b[`cZh\Y`ibXYfd]bb]b[`bUhifU``UbXd\mg]\W'`g\\Yb\W`g`UbX`h\Y`Yb[]bYYf]b[`ZbXUaYbhU`g'Udd`]\WV`Y`hc'h\Y`Yb[]bYYf]b[`X]g\\]d`]bY	
D9%"&"7cbWYdhi U``i bXYfgHJbX]b[ 'cZh\Y'a Uh\Ya Uh]Wgž'bi a Yf]WJ``UbU`mg]gž'gHJh]gh]Wgž'UbX Wca di hYf'UbX']bZcfa Uh]cb'gW]YbWYg'k\]W\`i bXYfd]b'h\Y'Yb[ ]bYYf]b[ 'X]gW]d`]bY	