

# **MECH9325**

: i bXUa YbHJ`gʻcZ5Wci gHJWg'/ 'Bc]gY

HYfa 'Hk c''##'&\$&%

# 7ci fgY<sup>-</sup>Cj Yfj ]Yk

## GHJZ7cbHJWh8YHJ]`g

#### 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWJhjcb	D\cbY
B]Wc`Y`?Ygg]ggc[`ci	b"_Ygg]ggc[`ci 4 i bgk "YXi "Ui	<u> </u>	F cca '(\$, ; ž @Y  Y`'(ž	
			5]bgk cfh	
			Vi ]`X]b[	

#### 8Ya cbghfUhcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWJhjcb	D\cbY
7 ]_U] <sup>:</sup> @ b	W <u>/_</u> U]"`]b4 i bgk "YXi "Ui			
F ca Ub '?]g`Yf	f"_]g`Yf4 i bgk "YXi "Ui			
I	[ mUb]g\Ub_Uf"g\Ufa U4 i bgk "YX			
G\Ufa U	i "Ui			
>YZFYmiDYb[	YZEYm'dYb[4 i bgk "YXi "Ui			

## GWXcc`7cbHJWhi±bZcfa Uhjcb

## @cWUh]cb

I BGK "A YWXUb]WU``UbX"A Ubi ZUWfi f]b[ '9b[ ]bYYf]b[

5]bgk cfh\ 'Vi ]`X]b[ '>%+ž'@Yj Y`'%

5Vcj Y '7 c ZZYY 'cb '7 Ua di g

#### < ci fg

-.\$\$-).\$\$da ž'A cbXUm-: f]XUm

ł7`cgYX'cb'di V']W\c`]XUmgž'GW\cc``gW\YXi `YX'Yj Ybhg'UbX'I b]j Yfg]hmG\i hXck b

#### K YV

#### GVX <u>@d/XccZA~YXXX UYb/[XVUIb]UVbX~IAbVXbA\_XUVVYiZE[Jvbyf\_1'9bd[\_1']bbYf/ft]bf[</u>

9b[]bYYf]b['Gh XYbhGi ddcfhGYfj]Wyg

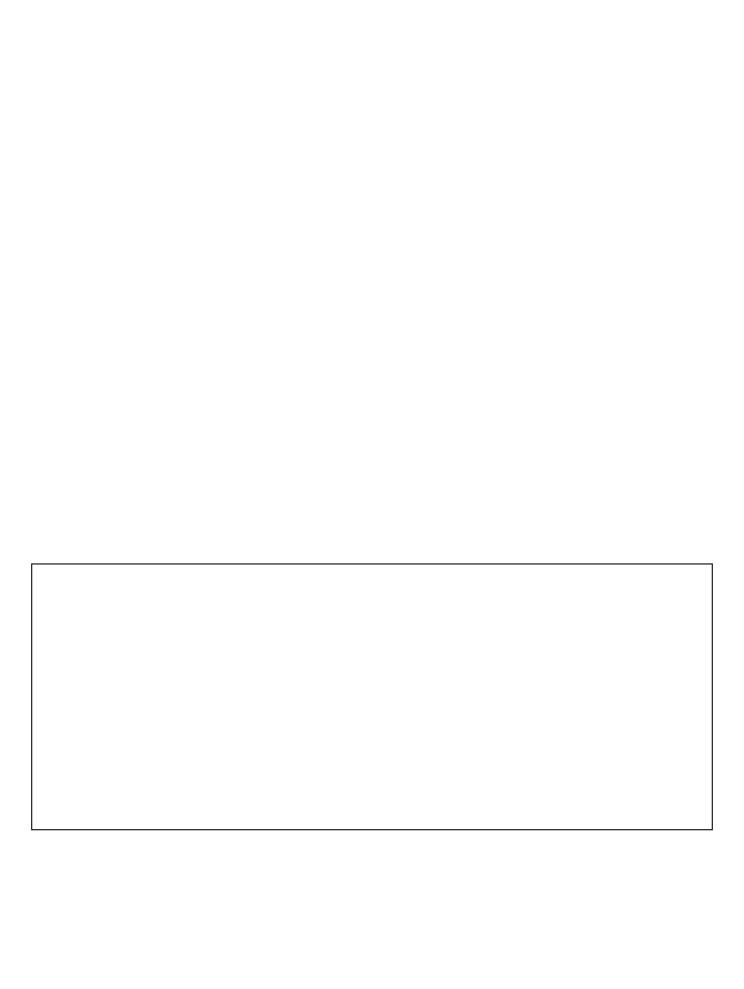
9b[]bYYf]b['\DXi glf]U\'HfU]b]b[

L B G K 'Ghi Xm'5 Vfc UX'Ub X'9 I VX Ub [ Y

fŽ\*%"&Ł"-',) ',) \$\$"—"Bi WYi g"Ghi XYbh'<i V

fŽ\*%%&L'-',) '' %+-'-'I BGK 'Gh Xm5VfcUX'UbX'I BGK '9| WXUb[Y'fZcf']bVci bX'gh XYbhgŁ

fĚ\*%°&Ł'-',) '(\$-+'-'GV\cc`'CZ]\\H



 $H\g`WcifgY`k\]```dfcj\]XY`Uk\UfYbYgg`cZbc]gY`UbX`]hg`[\YbYfUh]cb"`H\]g`WcifgY`]g`U`gc`]bhYbXYX`hc`[\]j\Y`mcih\Y`g_]``g`hc`a\YYhh\Y``YWifYXg`cZh\cgY`Ya\VUf_]b[\cb`U`WUfYYf`]b`UWcigh]Wg"`H\Y``YWifY`a\UhYf]U`ž'h\hcf]U`YI\YfW]gYg`UbX`U`j\Uf]YhmcZUggYgga\YbhUWhj\Jh]Yg`k\]```VY`[\]j\Yb"`\bj\JhYX`]bXi\ghfmiUWcigh]Wwcbgi`hUbhg`k\]``\[]j\Y`[\iy\ghfWg`UbX`bc]gY`]b`U`fUb[\Y`cZUdd`]WUh]cbg"`$ 

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. FYZYf'hc'h\Y'\UbXci h'Zcf'YUW\'`UV"

8YHJ]`g.

fUŁ@UV'%k]``Wca dUfY'X]ZZYfYbhXYgWf]dhcfg'Zcf'h]a Y'j Ufm]b['bc]gY"'@UV'&'k]``WJ'W'`UhY'h\Y'gci bX'dck Yf 'Yj Y`g'cZU'gci bX'gci fWY'Zfca 'gci bX'dfYggi fY'`Yj Y`a YUgi fYa Ybhg"

fl/k"H\YfY"UfY"hk c "UVg"

fWLH\Y``UVg`UfY`hc`VY`WcbXi WhYX`]bX]j ]Xi U``m'

fXŁ'5 a Uf\_]b[ 'fi Vf]Wk ]``'VY'dfcj ]XYX'Zcf'YUW\'`UV"

fYE'H\Y'XYUX`]bY'Zcf'UVgc`i hY'ZJ]``]g'cbY'k YY\_'UZhYf'h\Y'Xi Y'XUhY'Zcf'YUVX'`UV''

fZ-A Uf\_g·Zcf·YUWX·`UV`k]```VY`fYh fbYX`k]h\]b`&'kYY\_g`cZh\Y`XiY`XUhY"

Hk c ``UVg`k ]```VY`[ ]j Yb ]b h\ ]g`Wti fgY"'9UV\ ``UV`]g`k cfh\ '%\$i "'@UV`%`]g`Xi Y`Hi YgXUm&- '>i bY`) da "'@UV`& ]g`Xi Y`Hi YgXUm&\$'>i `m') da "

Gi Va ]gg]cb bchYg. j ]U A ccX`Y

Hi fb]h]b gYh]b[. `H\]g Ugg][ ba Ybh]g gi Va ]hhYX h\fci [\`Hi fb]h]b UbX gh XYbhg Xc bchgYY Hi fb]h]b g]a ]`Uf]hmfYdcfhg"

5ggYgga Ybh' . 5gg][ ba Ybh

GhUfhXUhY. Bch5dd`]WUV`Y

8 YHJ] g.

fUEH\Y`Ugg][ ba Ybh]g`h\Y`bi a Yf]WU`XYg][ b`cZU`gcb]WWfmghU``bc]gY`VUff]Yf''

fWEH\Y`Ugg][ ba Ybh`]g`Ub`]bX]j ]Xi U``UggYgga Ybh'

fXŁ'5 a Uf\_]b[ 'fi Vf]Wk ]``VY'dfcj ]XYX'Zcf'h\Y'Ugg][ ba Ybh'

fYŁH\Y'XYUX`]bY'Zcf'UVgc`i hY'ZJ]``]g'cbY'k YY\_'UZhYf'h\Y'Xi Y'XUhY'Zcf'YUW\'dUfhcZh\Y'Ugg][ ba Ybh'

fZ:A Uf\_q Zcf'h\Y Ugg][ ba Ybhk ]``VY fYh fbYX k ]h\]b %k YY\_cZh\Y Xi Y XUhY"

Gi Va ]gg]cb bchYg. j ]U A ccXY

Hi fb]h]b gYh]b[. H\]g ]g bchU Hi fb]h]b Ugg][ ba Ybh

5ggYgga Ybh'(.': ]bU`'9l Ua ]bUh]cb

@Yb[ h\.

# 5 hm/b XUbVW F Yei ]fYa Ybhg

 $\hbox{Ghi XYbhg."} \hbox{UfY."ghfcb[`mYbWc'i fU[YX'hc."UhhYbX."U```WUggYg."UbX'fYj.]Yk. ``YVWi fY'fYWcfX]b[g''] } \\$ 

# 7ci fgY GWX YXi `Y

# FYgci fWyg

## FYWca a YbXYX FYgci fWfg

FYWca a YbXYX'hYI hg`Zcf'h\]g'Wci fgYžk\]W\`UfY'Uj U]`UV`Y`]b`h\Y`I BGK 'Vcc\_g\cd'Ug'k Y```Ug'h\Y`I BGK`]VfUfmž'UfY``]ghYX'VY`ck.

Ga ]h\ž6">"žDYhYfgžF">"'UbX'Ck YbžG"'5Wci gh]Wg'UbX'bc]gY'Wcblfc`ž'&bX'YX]h]cbž5XX]gcb'K Yg`Ym@cb[a Ubž'% - \*"

B cfficbž A "D" 'UbX'? UfWhi Vž 8 ": i bXUa YbtU`gʻcZbc]gY`UbX'j ]VfUhJcb`UbU`mg]gʻZcf`Yb[]bYYfgž'&bX'9X]hJcbž 7 Ua Vf]X[Y'I b]j Yfg]mmDfYggž'7 Ua Vf]X[Yž'&\$\$' "

6]Ygž8":5"'UbX'<UbgYb'7"<"'9b[]bYYf]b['Bc]gY'7cblfc`.'H\Ycfm'UbX'DfUWf)WYž' fX'9X]h]cbž'9/: B'Gdcbž&\$\$'"

I gYZ ```]b\_g.

I BGK @|VfUfmk YVg]hY. \hdg.#k k k "\]VfUfm'i bgk "YXi "Ui #

A ccX`Y. '\hdg.##a ccX`Y"hY`h'i bgk "YXi "Ui #c[]b#bXYI "d\d

#### HYUa q.

#### 7 ci fgY '9j U'i Uhcb 'UbX '8 Yj Y'cda Ybh

: YYXVUW\_cb'h\Y'Wci fgY']g'[Uh\YfYX'dYf]cX]WJ``mi g]b['j Uf]ci g'a YUbgž']bWi X]b['h\Y'I BGK a m9I dYf]YbW''dfcW'ggž']bZcfa U``X]gW gg]cb']b'WUggž'UbX'Uh'h\Y'GW\cc``gh XYbh#ghUZZa YYh]b[g"'Mci f ZYYXVUW\_']g'hU\_Yb'gYf]ci g`m'' 7 cbh]bi U``]a dfcj Ya Ybhg'UfY'a UXY'hc'h\Y'Wci fgY'VUgYXž']b'dUfhž'cb'mci f ZYYXVUW''

## Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

## 5ggYgga Ybhgi Va ]gg]cb UbX a Uf\_]b[ Wf]hYf]U

G\ci`X'h\Y'WcifgY'\UjY'Ubmbcb!Y`YWfcb]WUggYgga Ybhigi Va ]gg]cbž'h\YgY'g\ci`X'\UjY'U'ghUbXUfX GW\cc`WcjYf'g\YYh'

5```gi Va ]gg]cbg`UfY`YI dYWYX`hc`VY`bYUh`UbX`WYUf`mgYhci h'`Mci f`fYgi `hg`UfY`h\Y`d]bbUWY`cZU```mci f`\UfX k cf\_'UbX`g\ci `X`VY`hfYUhYX`k ]h\`Xi Y`fYgdYWf`DfYgYbh]b[ `fYgi `hg`WYUf`m[ ]j Yg`h\Y`a Uf\_Yf`h\Y`VYghW\UbW\ cZi bXYfghUbX]b[ `mci f`a Yh\cX/Yj Yb`]Zh\Y`bi a Yf]WU``fYgi `hg`UfY`]bWcffYWf

A Uf\_]b[ '[ i ]XY`]bYg`Zcf`Ugg][ ba Ybhgi Va ]gg]cbg`k ]```VY`dfcj ]XYX`Uhh\Y`gUa Y`h]a Y`Ug`Ugg][ ba YbhXYhU]`g hc`Ugg]ghk ]h\`a YYh]b[ 'UggYggUV`Y`fYei ]fYa Ybhg"`Gi Va ]gg]cbg`k ]```VY`a Uf\_YX`UVWcfX]b[ 'hc`h\Y`a Uf\_]b[ [ i ]XY`]bYg`dfcj ]XYX"

#### @UhY 'dc`]Wh

K cf\_'gi Va ]hhYX``UhY`k ]h\ci hUb`Uddfcj YX`YI hYbg]cb`Vmh\Y`Wci fgY`WcfX]bUhcf`cf`XY`Y[ UhYX`Ui h\cf]hm]g gi VYWhhc`U``UhY`dYbU`hmcZ&\$`dYfWYbhf&\$i \ \!cZh\Y`a Ul ]a i a 'a Uf\_'dcgg]V`Y`Zcf`h\UhUggYgga Ybh]hYa ž dYf`WU`YbXUf`XUm'

 $\label{eq:conversion} \text{K cf\_'gi Va ]} \text{httx:'UZhtf:h.Y:'XYUX`]bY:'Zcf:'UVgc`i htt:'ZU]'':]g'bchUWWtdhtx:'UbX:'U'a Uf\_'cZ'nYfc'k ]```VY'Uk UfXYX Zcf:'h.Uh'UggYgga Ybh']hta " } \\$ 

: cf`gca Y`UggYgga Ybh`]hYa gž`U``UhY`dYbU`hma UmbchVY`Uddfcdf]UhY"`H\YgY`UfY`WYUf`m`]bX]\WUhYX`]b`h\Y Wci fgY`ci h`]bYž`UbX`gi W\`UggYgga Ybhg`fYWY]j Y`U`a Uf\_`cZnYfc`]ZbchWca d`YhYX`Vmh\Y`gdY\\JZ]YX`XUhY" 9I Ua d`Yq`]bWi XY.

%" K YY\_`mcb`]bY`hYghg`cf``UVcfUhcfmk cf\_`k cfh\`U`ga U```dfcdcfh]cb`cZh\Y`gi VYWha Uf\_žcf &" C b`]bY`ei ]nnYg`k \YfY`Ubgk Yfg`UfY`fY`YUgYX`hc`gh XYbhg`cb`Wca d`Yh]cbžcf

- "DfcZYgg]cbU``UggYgga YbhihUg\_gž'k\YfY`h\Y`]bhYbh]cb`]g`hc`WfYUhY`Ub`Ui h\Ybh]WUggYgga Ybhih\Uh\Ug`Ub`UVgc`i hY`gi Va ]gg]cb`XUhYž'cf
- ("DUgg# U]`UggYgga YbhHJg\_g"

## 91 Ua ]bUh]cbg

UggYgga YbhidYfZcfa UbWYžmci 'UfY'Y`][]V`Y`hc'Udd`m'Zcf'GdYWJU``7cbg]XYfUhJcb'df]cf'hc'gi Va]htjb['UbUggYgga Ybhicf'g]htjb['Ub'Yl Ua"

: cf`XYhJ]`g`cZUdd`m]b[ 'Zcf`GdYW]U``7 cbg]XYfUh]cb`UbX`WcbX]h]cbg`Zcf`h\Y`Uk UfX`cZgi dd`Ya YbhUfm UggYgga Ybhž'd`YUgY`gYY`h\Y`]bZcfa Uh]cb`cb`I BGK 'g`<u>GdYWU``7 cbg]XYfUh]cb`dU[Y</u>"

D`YUgY'bchY'h\Uhghi XYbhg'k]``bch'VY'fYei]fYX'hc'dfcj]XY'Ubm'XcW'a YbhUfm'Yj]XYbWY'hc gi ddcfh'UVgYbWg'Zfca 'Ubm'WUggYg'a]ggYX'**VYWUi gY'cZ'7CJ=8!%** 'di V`]W\YU'h\ 'a YUgi fYg'gi W\'Ug]gc`Uh]cb"'| BGK 'k]``bch'VY']bg]gh]b[ 'cb'a YX]WU`'VW'fh]ZJWUh'Yg'Zfca 'UbmcbY'XYYa YX'hc'VY'U'dcg]h]j Y'WUgYZ cf'k\Yb'h\Ym\Uj Y'fYWcj YfYX"'Gi W\'WYfh]ZJWUh'Yg'UfY'X]ZZJW 'hhc'cVhU]b'UbX'di h'Ub'i bbYWYggUfmghfU]b'cb ghi XYbhg'UbX'a YX]WU`'ghUZZ''

 $5\,dd^{3}WUhlcbg^{3}Zcf^{3}gdYW_{U}^{3}W^{3}bg^{3}XYfUhlcb^{3}k^{3}XYfUhlcb^{3}xYfUh$ 

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

 $\label{thm:continuous} IBGK ``Ug`Ub`cb[c]b[`Wcaa]haYbhhc`ZcghYf]b[``U`W``hifY`cZ`YUfb]b[`]bZcfaYX`VmUWUXYa]W]bHY[f]hm'`5``IBGK ``ghiXYbhg``UjY`U`fYgdcbg]V]`]hmhc`UX\YfY`hc`h\]g`df]bW]d`Y`cZUWUXYa]W]bHY[f]hm'`D`U[]Uf]gaibXYfa]bYg`UWUXYa]W]bHY[f]hmUbX`]g`bchhc`YfUhYX`UhIBGK "`B'SY[Sde_SfG@EI[eVWY] WW Sege[YfZWiadVead[VWSeaXafZWbeS`VbSee[YfZW_aXXSekagdai`ž$ 

Mci 'UfY'U'gc'fYa ]bXYX'h\UhWUfYZ ``h]a Y'a UbU[ Ya Ybh]g'Ub']a dcftUbhdUfhcZgh XmUbX'cbY'cZh\Y ]XYbh]Z]YX'WUi gYg'cZd`U[ ]Uf]ga ']g'dccf'h]a Y'a UbU[ Ya Ybh'Gh XYbhg'g\ci `X'U``ck 'gi Z]W]Ybh'h]a Y'Zcf fYgYUfW\žXfUZ\]b[ 'UbX'h\Y'dfcdYf'fYZYfYbW]b[ 'cZgci fWYg']b'dfYdUf]b[ 'U``'UggYgga Ybh'lUg\_g''

₹d`U[]Uf]ga `]g`Zci bX`]b`mci f`k cf\_k \Yb`mci `UfY`]b`Z[fghmYUfžmci f``YWh fYf`k]``cZYf`mci `Ugg]ghUbWY`hc
]a dfcj Y`mci f`UWUXYa]Wg\_]``g"`H\Yma UmUg\_mci hc``cc\_Uhgca Y`cb`]bY`fYgci fWygžUhhYbX`h\Y`@YUfb]b[
7 YbhfYžcf`gca Yh]a Yg`fYgi Va]hmci f`k cf\_k]h\`h\Y`dfcV`Ya `Z[|YX"'<ck Yj Yf`a cfY`gYf]ci g`]bghUbWyg`]b`Z[fgh
mYUfžgi W\`Ug`ghYU`]b[`Ubch\Yf`gh XYbhg`k cf\_cf`dUm]b[`gca YcbY`hc`Xc`mci f`k cf\_ža UmVY`]bj Ygh][UhYXhUg\_g"

# 5WUXYa]W±bZcfaUhjcb

# 7 fYX]hdc]bhg

 $7\,ci\,fgY\,'WfYX]hi]g\,'WU\,'W'\,'Uh'X\,']b\,'I\,\,b]hg!\,C\,Z\,7\,fYX]hfl\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,C\,(A)$ 

- A ccX`Y
- <u>@UV'5WWYgg</u> 7 ca di hb[': UW]hYg

# 5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

Dfc[fUa '±bhYbXYX'@YUfb]b['CihWca Yg	