

# **MMAN4010**

H\Yg]g<sup>·</sup>5

HYfa 'Hk c''##'&\$&%

# 7ci fgY<sup>·</sup>Cj Yfj ]Yk

## GhJZZ 7 cbhJWh 8 YhJ] `g

## 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
5b[ '@ i	Ub[ "`]i 4 i bgk "YXi "Ui		>%+!(\$,	Ž*% &!-',)(
	_			\$, \$

## 8Ya cbghfUhcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWJhjcb	D\cbY
5`] <sup>.</sup> 5\a YX	U"Z'U\a YX4 i bgk "YXi "Ui			
6ca ]b[ 'N\Ub[	Vca ]b[ "n\Ub[ 4 i bgk "YXi "Ui			
MJb.K Np[	mUb"k Ub[-4 i bgk "YXi "Ui			
Ai∖UaaUX <sup>-</sup> -afUb	ai\UaaUX"]afUb4ibgk"YXi"U			

fŽ\*%'&Ł'-',)'+\*\*%-'9b[]bYYf]b['+bXi ghf]U`'HfU]b]b[

fŽ\*%'&Ł'-',)''%+-'-'I BGK 'Ghi Xm'5VfcUX'UbX'I BGK '9I W\Ub[Y'fZcf']bVci bX'ghi XYbhgŁ

fŽ\*%'&Ł'-',)'(\$-+'-'GW\\cc`'C ZZ\W\H

łłD`YUgY bchY h\Uhih\Y GW\cc`'C Z]WY k]``bch\_bck k\Yb#Zmci f'Wci fgY Wcbj Ybcf']g'cb'WUa di g'cf Uj U]`UV`Y

## 9a U]`

9b[]bYYf]b['Gh XYbhGi ddcfhGYfj ]Wg - W ffYbhgh XYbhYbei ]f]Yg

• Y"[""Ybfc`a Ybhž'dfc[fYgg]cbž'WUg\"fYei Yghgž'Wci fgY']ggi Yg'cf'dfc[fUa!fY`UhYX'ei Yf]Yg

<u>9b[]bYYf]b['±bXi glf]U`'HfU]b]b[</u>'-'±bXi glf]U`'lfU]b]b[ 'ei Ygl]cbg

<u>I\_BGK\_'Gh\_Xm5VfcUX</u>'--gh\_XmUVfcUX'gh\_XYbhYbei\_]f]Yg\_fZcf']bVci\_bX'gh\_XYbhgŁ

<u>I BGK '91 WXUb[Y</u>'-gh XYbhYl WXUb[Y'Ybei]f]Yg'fZcf']bVci bX'gh XYbhgŁ

I BGK : i h fY Gh XYbhg - dch bh U gh XYbh Ybei ]f] Yg

• Y"["UXa]gg]cbgžZYYgždfc[fUagžWfYX]hlfUbgZYf

<u>GWkcc``CZJWY</u>'-GWkcc``[YbYfU``cZJWY'UXa]b]ghfUh]cb'Ybei]f]Yg

## 7ci fgY 8YHJ] g

### 7 fYX]h'Dc]bhg'\*

## Gi a a UfmcZh\Y 7ci fgY

Gh XYbhgʻg\ci `X`\Uj YʻdUggYX`% &`i b]hgʻUhih\Yʻh]a Yʻh\YmVca a YbVVʻh\]gʻVci fgY"`

### 7 ci fgY 5]a g

#### 7ci fgY 5]a g

H\]g`Wci fgY`Yb\UbWrg`h\Y`gh XYbhg`g\_]``g`Zcf`i bXYfhU\_]b[ `gWkc`Uf`miYbei ]fmVmUhhYa dh]b[ `hc`UWk]Yj Y`U gdYW]ZJWhcd]WcVYWfj Y`k ]h\]b`U`XYZJbYX`dYf]cX`cZh]a Y"`5`g][ b]ZJWUbhWca dcbYbhcZh\Y`Wci fgY`fY`UhYg`hc h\Y`fYj ]Yk `cZ`]hYfUhi fYžk\]W\`dfca chYg`]bXYdYbXYbhUbX`fYZYWfj Y``YUfb]b[ `Ug`k Y```Ug`]bWfYUgYg ghi XYbhg`'WUdUW]mhc`XYj Y`cd`]bZcfa Uh]cb``]hYfUWh''`H\Y`h\Yg]g`]g`YI dYWhYX`hc`fY]bZcfWY`h\Y`ghi XYbhg`UV]`]hm UbX`WcbZJXYbWY`]b`h\Y`k f]hHYb`Wca a i b]WUh]cb`cZhYWkb]WU`]bZcfa Uh]cb"

### 7 ci fgY @YUfb]b[ Ci hWca Yg

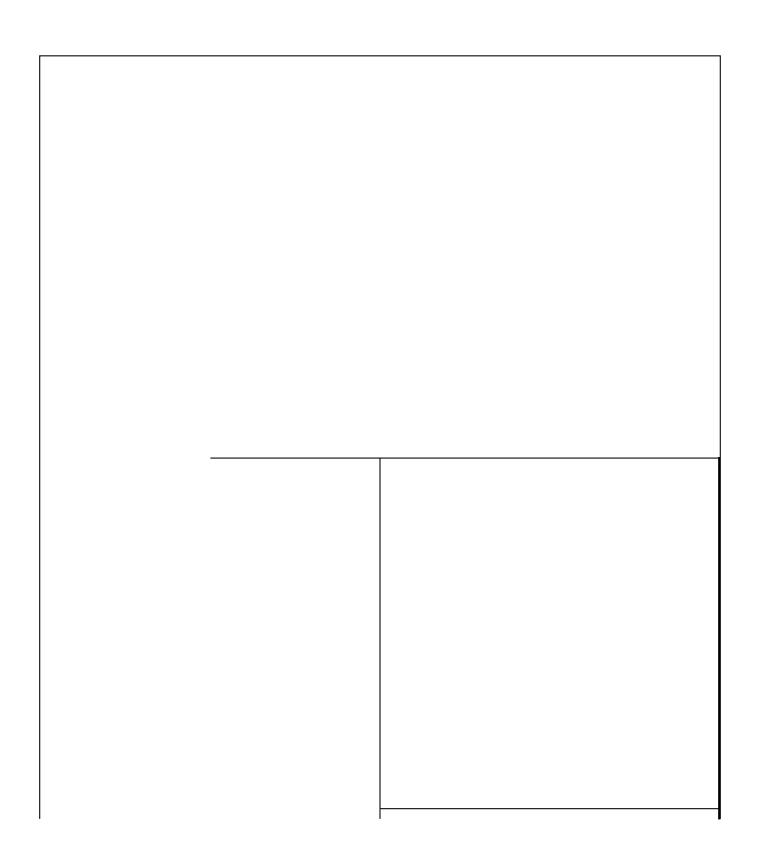
5 ZYfgi WWgqZ ``mWa d`YNb['h\]g'Wa fqYžmci 'g\ci `X'VY'UV`Y'hc.

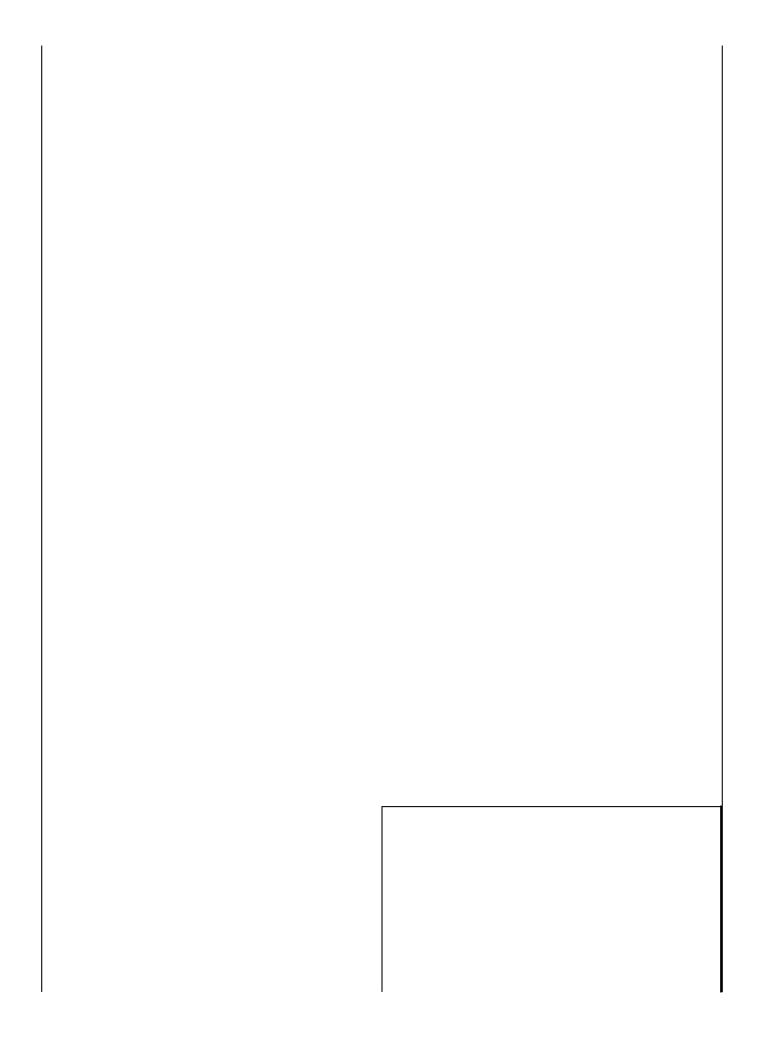
@YUfb]b[ 'Ci HWca Y	95 GW[Y %7ca dYMbW]Yg
%":7cbXi Whi]bXYdYbXYbhifYgYUfWX:UbX:Udd`mYgHUV`]g\YX:h\Ycf]Yg hc:UXXfYgg:Ub:Yb[]bYYf]b[:dfcV`Ya:h\UhXcYg:bch\Uj Y:U'k Y``! XYZ]bYX:gc`i h]cb	D9&"' ž'D9&"( ž'D9' "%
&"`5bU`mgY`Wf]h]WU``mžfYZYWicb`UbX`gmbh\Yg]gY`Wcad`YI ]bZcfaUh]cbždfcV`YagžWcbWdhg`UbX`h\Ycf]Yg	D9%" ž'D9%"(
' "`=bHYfdfYhUbX`lfUbga ]h_bck `YX[ Yž`g_]``g`UbX`]XYUg`hc`gdYW]U`]gh UbX`bc!gdYW]U`]ghUi X]YbWYg	D9&"%ŽD9&"&
("'8Ya cbghfUhY'a UbU[Yf]U`'g_]``g'UbX']bX]j ]Xi U``fYgdcbg]V]`]hmhc Wca d`YhY'U'dfcYWhk ]h\]b'``]a ]hYX'hJa Y'UbX'fYgci fWfg	D9' "&ž'D9' "( ž'D9' ") ž'D9' "*

## HYUWX]b[ GhfUhY[]Yg

H\Y'H\Yg]g`]g`k\YfY`YUWX`ghi XYbhik cf\_g`i bXYf`h\Y`[i]XUbWY`cZUWUXYa]WghUZk]h\`]bdi hZfca `hYWXb]WU`f]bXi ghfn#YgYUfWX#dfUWf]h]cbYfL`gdYWJU`]ghg"`Hcd]Wg`UfY`fY`UhYX`hc`dfcYWfg`gY`YWYX`Zfca `WcbhYa dcfUfm dfUWf]WY"`H\Y`k cf\_`]bj c`j Yg`fYgYUfWX!VUgYX`]bj Ygh[[Uh]cbgž]bXi ghf]U``dfcV`Ya g`UbX`XYg][b`Udd`]WUh]cbg"







## FYgci fWyg

### FYWca a YbXYX FYgci fW/g

U" I BGK @|VfUfmik YVg]|Y. `\hdg.#k k k "`]VfUfmii bgk "YXi "Ui #V" A ccX`Y. `\hdg.#a ccX`Y"hY`hii bgk "YXi "Ui #c[]b#|bXYI "d\d

### 7ci fgY 9j U'i Uh]cb UbX 8Yj Y'cda Ybh

: YYXVUW\_cb`h\Y`Wci fgY`]g`[ Uh\YfYX`dYf]cX]WU``mi g]b[ 'j Uf]ci g`a YUbgž]bWi X]b[ 'h\Y`I BGK a m9l dYf]YbW'`dfcW'ggž]bZcfa U``X]gW gg]cb`]b`h\Y`Z]bU``WUgg`Zcf`h\Y`Wci fgYžUbX`h\Y`GW\cc`'g Gh XYbh#GhUZZa YYh]b[ g"`Mci f`ZYYXVUW\_`]g`hU\_Yb`gYf]ci g`mžUbX`Wcbh]bi U``]a dfcj Ya Ybhg`UfY`a UXY`hc`h\Y Wci fgY`VUgYXž]b`dUfhžcb`gi W\`ZYYXVUW\_"

#5 'th\]g'Wci fgYz'fYWYbh']a dfcj Ya Ybhg'fYgi `h]b[ 'Zfca 'ghi XYbh'ZYYXVUW\_']bWi XY. '[ fci d'Zcfa Uh]cb'k ]h\]b h hcf]U`gYgg]cbz'[ fUX]b[ 'dfcWYXi fY 'UbX'a YW\Ub]ga z'XcW a YbhUh]cb'cZgdYW]U`'UffUb[ Ya Ybh'VYhk YYbYUW\] fci d'k ]h\'h\Y'hYUW\]b[ 'hYUa z'

UggYgga YbhidYfZcfa UbWYžmci 'UfY'Y`][]V`Y`hc'Udd`m'Zcf'GdYWJU``7cbg]XYfUhJcb'df]cf'hc'gi Va]hhJb['UbUggYgga Ybhicf'g]hhJb['Ub'Yl Ua"

: cf`XYhJ]`g`cZUdd`m]b[ 'Zcf`GdYW]U``7 cbg]XYfUh]cb`UbX`WcbX]h]cbg`Zcf`h\Y`Uk UfX`cZgi dd`Ya YbhUfm UggYgga Ybhž'd`YUgY`gYY`h\Y`]bZcfa Uh]cb`cb`I BGK 'g`<u>GdYWJU``7 cbg]XYfUh]cb`dU[Y</u>"

D`YUgY'bchY'h\Uhghi XYbhg'k]``bch'VY'fYei]fYX'hc'dfcj]XY'Ubm'XcW'a YbhUfm'Yj]XYbWY'hc gi ddcfh'UVgYbWg'Zfca 'Ubm'WUggYg'a]ggYX'**VYWUi gY'cZ'7CJ=8!%** 'di V`]W\YU'h\ 'a YUgi fYg'gi W\'Ug]gc`Uh]cb"'| BGK 'k]``bch'VY']bg]gh]b[ 'cb'a YX]WU`'VW'fh]ZJWUh'Yg'Zfca 'UbmcbY'XYYa YX'hc'VY'U'dcg]h]j Y'WUgYZ cf'k\Yb'h\Ym\Uj Y'fYWcj YfYX"'Gi W\'WYfh]ZJWUh'Yg'UfY'X]ZZJW 'hhc'cVhU]b'UbX'di h'Ub'i bbYWYggUfmghfU]b'cb ghi XYbhg'UbX'a YX]WU`'ghUZZ''

 $5\,dd^{3}WUhlcbg^{3}Zcf^{3}gdYW_{U}^{3}W^{3}bg^{3}XYfUhlcb^{3}k^{3}XYfUhlcb^{3}XYfUhlcb^{3}xYfUhlcb^{3}xYfUhlcb^{3}XYfUh$ 

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

 $\label{thm:continuous} IBGK ``Ug`Ub`cb[c]b[`Wcaa]haYbhhc`ZcghYf]b[``U`W``hifY`cZ`YUfb]b[`]bZcfaYX`VmUWUXYa]W]bHY[f]hm'`5``IBGK ``ghiXYbhg``UjY`U`fYgdcbg]V]`]hmhc`UX\YfY`hc`h\]g`df]bW]d`Y`cZUWUXYa]W]bHY[f]hm'`D`U[]Uf]gaibXYfa]bYg`UWUXYa]W]bHY[f]hmUbX`]g`bchhc`YfUhYX`UhIBGK "`B'SY[Sde_SfG@EI[eVWY] WWSege[YfZW_aXSekagdai`ž$ 

Mci 'UfY'U'gc'fYa ]bXYX'h\UhWUfYZ ``h]a Y'a UbU[Ya Ybh]g'Ub']a dcftUbhdUfhcZgh XmUbX'cbY'cZh\Y ]XYbh]Z]YX'Wai gYg'dXdd[]Uf]ga ']g'dccf'h]a Y'a UbU[**%a** Ybh'Gh XY**%a**g'g\**%**X'U``ck 'gi Z]W]Ybh'h]a Y'Zcf fYgYUfW\žXfUZ\]b['UbX'h\Y'dfcdYf'fYZYfYbW]b['cZgci fWYg']b'dfYdUf]b['U``'UggYgga Ybh'lUg\_g''

⊋d`U[]Uf]ga i]gʻZci bXi]bimci fik cf\_ik \Ybimci i'UfYi]biZ[fghmYUfžimci fi`YWhi fYfik]``cZYfimci i'Ugg]ghUbWYihc ]a dfcj Yimci fi'UWUXYa]Wg\_]``g'''H\Yma UmUg\_imci ihc ``cc\_'Uhigca Yicb`]bYifYgci fWYgž'UhhYbXih\Yi@YUfb]b[ 7 YbhfYžcfigca Yh]a YgifYgi Va]himci fik cf\_ik]h\ih\YidfcV`Ya iZ[l YX'''<ck Yj Yfia cfYigYf]ci gi]bghUbWYgi]biZ[fgh mYUfžgi W\iUgighYUi]b[i'Ubch\Yfighi XYbhgik cf\_icfidUm]b[i'gca YcbYihciXcimci fik cf\_žcc\_ib

## 5WUXYa]W±bZcfaUhjcb

## 7 fYX]hdc]bhg

 $7\,ci\,fgY\,'WfYX]hi]g\,'WU\,'W'\,'Uh'X\,']b\,'I\,\,b]hg!\,C\,Z\,7\,fYX]hfl\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,cf\_`cUX\,'YI\,\,dYWfUh]cb\,'Zcf'cbY\,'I\,\,C\,7\,L''\,'H\,\backslash\,Y\,'bcfa\,\,U\,''k\,\,C\,(A)$ 

- A ccX`Y
- <u>@UV'5WWYgg</u> 7 ca di hb[': UW]hYg