

**MATHEMATICS ENRICHMENT CLUB.**

**Problem Sheet 2, May 13, 2014<sup>1</sup>**

1. (a) Show that 120 is a divisor of  $n^5 - 5n^3 + 4n$  for every integer  $n$ .  
(b) Show that 49 is not a divisor of  $n^2 + n + 2$  for every integer  $n$ .
2. Three people,  $A$ ,  $B$  and  $C$ , entered a competition. After the event,  $A$  reported " $B$  was second,  $C$  was first".  $B$  said, " $A$  was second,  $C$  was third".  $C$  said, " $A$  was first,  $B$  was third". Each person's report contained one true statement and one false one. Which of  $A$  and  $B$  performed better in the competition.
- 3.

5. Find all pairs of integers  $x$  and  $y$  such that  $x^3 - y^3 = 1729$ . Show that there are no others.

6.