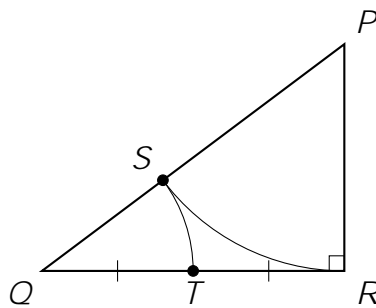


MATHEMATICS ENRICHMENT CLUB.  
Problem Sheet 15, September 10, 2019

1. *AMC 2012 Senior Division, Q12.*

Triangle  $PQR$  is right-angled at  $R$ . The circle with centre  $P$  and radius  $PR$  cuts  $PQ$  at  $S$  and the circle with centre  $Q$  and radius  $QS$  cuts  $QR$  at  $T$ .



If  $T$  bisects  $QR$ , find the ratio  $QS : SP$ .

2. Find all possible solutions to

$$\frac{x}{y} + \frac{1}{x} + \frac{1}{y} = \frac{1}{4}$$

if  $x$  and  $y$

### Senior Questions

1. The triangular numbers are given by  $T_n = 1 + 2 + \dots + n$  for  $n$  a positive integer ( $T_1 = 1$ ).

Discover and prove a formula for

$$T_n \left( \frac{1}{T_1} + \frac{1}{T_2} + \dots + \frac{1}{T_n} \right) :$$

2.  $A, B, C$  and  $D$  are points on the parabola  $y = x^2$  such that  $AB$  and  $CD$  intersect on the  $y$ -axis. Determine the  $x$ -coordinate of  $D$  in terms of the  $x$ -coordinates of  $A, B$  and  $C$ , which are  $a, b$  and  $c$  respectively.