MATHEMATICS ENRICHMENT CLUB. Problem Sheet 8, June 24, 2019

1. Given that x and y are integers, how many different solutions are there to the equation

$$jxj + 2jyj = 100?$$

2. Place the numbers 1;2;4;8;16;32;64;128 and 256 in a 3 3 square grid in such a way,

Senior Questions

1. How many di erent integers x satisfy the equation

$$(x^2 5x + 5)^{x^2 11x + 30} = 1?$$

- 2. The integers 5, 11, 17, 23 and 29 are ve prime numbers in arithmetic progression. Find *six* prime numbers in arithmetic progression.
- 3. Given that n is a positive integer and 2n + 1 and 3n + 1 are perfect squares, prove that n is divisible by 40.